

## Extensions & Applications Topic 1: Density, Accessibility, Retail Models

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# Outline

- Population Density Models
- Accessibility and Potential Once Again
- The Retail Model: The Lakshmanan and Hansen, and the Huff Model
- Extending the Retail Model to Deal with Agglomeration and Scale
- Calibrating and Validating Spatial interaction Models

## **Population Density Models**

We can simplify spatial interaction models and derive related structures and we have already looked at one of these which is potential or accessibility. There is a second one which is population density and we will introduce this and also repeat our accessibility measures to tie up loose ends

From the late 19th century or even before scholars observed that population densities fall as the distance from the central business district increase. Colin Clark in 1951 wrote a famous paper on this. In it he showed that population density called  $\rho_j$  from the CBD to some location j varied inversely with distance or travel cost  $C_j$ . He argued that this was a negative exponential function and the equation is

$$\rho_j \sim \exp(-\lambda c_j) = K \exp(-\lambda c_j)$$

This looks like a gravity model and we can get the model as follows from our standard – unconstrained – spatial interaction equation

$$T_{ij} = T \frac{O_i D_j \exp(-\lambda c_{ij})}{\sum_i \sum_j O_i D_j \exp(-\lambda c_{ij})}$$

Now note we have only one origin so  $O_i = Z$ . Only one set of transport costs from i, that is  $c_{ij} = c_j$ . And we assume that the destination attraction  $D_j = 1$ and this is somewhat consistent with the fact we are dealing with a density not a count. And then our spatial interaction model equation becomes

$$T_{j} = T \frac{\exp(-\lambda c_{j})}{\sum_{i} \sum_{j} \exp(-\lambda c_{j})} = \frac{T}{Z} \exp(-\lambda c_{j}) \sim \rho_{j} = K \exp(-\lambda c_{j})$$

which is the same as Clark's model

Now we can also very easily fit this model using regression – it is one dependent variable density and one independent variable transport cost and this if we take logs we get

$$\log \rho_j = \log K - \lambda c_j$$

Note that if we have an inverse power and not a negative exponential cost function we get

$$\log \rho_j = \log K - \lambda \log c_j$$

Here are some empirical applications from London Basically we have plotted the raw data trips and travel costs and then the logs of these assuming and inverse power. Then we have done the same by normalising dividing through by the employment and population to get trips densities; first for the basic data then for the logged data



Correlation -.1650 Regression Slope 7.563 Regression Intercept 7.442 % Mean Absolute Error 173.6



Correlation -.4401 Regression Slope 2.277 Regression Intercept 1.705 % Mean Absolute Error 42.50



Correlation-.1466Regression Slope.3368Regression Intercept28.92% Mean Absolute Error798.1



Correlation-.3254Regression Slope2.461Regression Intercept2.767% Mean Absolute Error -172.5

#### **Accessibility and Potential Once Again**

Again our spatial interaction model can be written as

$$T_{ij} = T \frac{O_i D_j \exp(-\lambda c_{ij})}{\sum_i \sum_j O_i D_j \exp(-\lambda c_{ij})} = T \frac{O_i D_j \exp(-\lambda c_{ij})}{Q}$$

Now if we add over i or j, we get two different potentials or accessibilities

$$V_j = \frac{T}{Q} D_j \sum_i O_i \exp(-\lambda c_{ij})$$

$$V_i = \frac{T}{Q} O_i \sum_j D_j \exp(-\lambda c_{ij})$$

Which can be simplified and normalised as potentials

or accessibilities per head – or in fact potential densities

$$v_{j} = \frac{V_{j}}{D_{j}} = \frac{T}{Q} \sum_{i} O_{i} \exp(-\lambda c_{ij}) \sim \sum_{i} O_{i} \exp(-\lambda c_{ij})$$
$$v_{i} = \frac{V_{i}}{D_{i}} = \frac{T}{Q} \sum_{i} D_{i} \exp(-\lambda c_{ii}) \sim \sum_{i} D_{i} \exp(-\lambda c_{ii})$$

 $O_i \quad Q \stackrel{\frown}{=} i$ 

And now I will show some maps of these – where you can see that accessibilities and densities and normalising factors are more or less the same in gravity density type models – I have shown you these before when I ran the Tyndall model a couple of weeks ago in the first lecture but here they are again



# The Retail Model: The Lakshmanan and Hansen, and the Huff Model

Ok the retail model is one of the most widely used singly constrained models. Essentially if distributes trips from home to retail measured as trip flows, or expenditure, or as employment needed in the retail sector to make the sector function. There are variants of all these measures in such applications and there is a very loose assumption that such variables are correlated.

We define the singly constrained model as usual as:

$$S_{ij} = \eta P_i \frac{F_j \exp(-\beta c_{ij})}{\sum_{i} F_j \exp(-\beta c_{ij})}$$

This is subject to an origin constraint which is

$$\sum_{j} S_{ij} = \eta P_i$$

And the amount of flow into the retail centre is given as the destination sum. Note that origins and destinations have been switched in terms of their notation – population is not the origin and retail employment the destination

$$\sum_{i} S_{ij} = S_{j}$$

That is all there is to it – note  $F_j$  is floorspace usually

# Extending the Retail Model to Deal with Agglomeration and Scale

Now we can extend it in two ways – first we can add a scaling factor to the attraction on the assumption that as a centre gets bigger, then it has economies of scale. I don't know if Elsa or anyone else has talked much about economies of scale but basically the assumption in economics is that as things get bigger other quantities grow more than proportionately – superlinearly. Thus we can replace

$$F_j \longrightarrow \longrightarrow F_j^{\alpha}$$

The model thus becomes

$$S_{ij} = \eta P_i \frac{F_j^{\alpha} \exp(-\beta c_{ij})}{\sum_j F_j^{\alpha} \exp(-\beta c_{ij})}$$

And in fact I think that one of Adam's exercises has this kind of scaling factor but to estimate it you would need multiple regression because there are two parameters – in fact three including the intercept,

Now we don't calibrate it this way as we will show in a minute but first we need to add an even more appropriate agglomerative effect by taking account of local economies of scales inside a retail centre

We can argue that local shops in a centre exert a positive effect on agglomeration by assuming that the attraction of the centre takes account of these local shops. If we now think of  $F_j^{\alpha}$  as a shop not a set of shops and note that there are other shops  $F_k^{\alpha}$  in the centre j then we can add up the effect of these shops on the attraction using a similar deterrence effect as

$$A_{j} = F_{j}^{\alpha} + \sum_{k \in \Omega_{j}} F_{k}^{\alpha} \exp(-\phi c_{jk})$$

Note we are summing over all the k located shops in the centre j and assuming a deterrent effect – i.e. closer shops exert of a positive effect Putting this into the model, we get an augmented retail model with three scaling parameter and of course some sort of constants to ensure normalisation. The model now looks like this  $F_i^{\alpha}$ 

$$S_{ij} = \eta P_i \frac{A_j \exp(-\beta c_{ij})}{\sum_j A_j \exp(-\beta c_{ij})} = \eta P_i \frac{\left[F_j^{\alpha} + \sum_{k \in \Omega_j} F_k^{\alpha} \exp(-\phi c_{jk})\right] \exp(-\beta c_{ij})}{\sum_j \left[F_j^{\alpha} + \sum_{k \in \Omega_j} F_k^{\alpha} \exp(-\phi c_{jk})\right] \exp(-\beta c_{ij})}$$

Of course we don't know what sign these parameters can take and it may be that the local effect is truly agglomerative and the parameter is positive

# Calibrating and Validating Spatial interaction Models

Now one of the problems we have is getting these parameter values and most of these kinds of models are non-linear – so we can't really take logs because the constant terms of are summations and relevant to origins or destinations or both. However the parameters apply to the whole system and therefore we can't use simple methods like regression.

So what we have to do is develop an iterative method – almost like trial and error to get the parameters

Basically to cut a long story short we need to define for each parameter – not for the normalising terms but for the system parameters distinct statistics that have to be met – these are usually features or properties of the distribution like means and variances and so on which the model has to meet.

In the case of the simpler retail model which is

$$S_{ij} = \eta P_i \frac{F_j^{\alpha} \exp(-\beta c_{ij})}{\sum_i F_j^{\alpha} \exp(-\beta c_{ij})}$$

We have to choose as follows ----

Choose  $\alpha$  so that

$$\sum_{i} \sum_{j} S_{ij} F_{j} = known \ value$$

And choose  $\beta$  so that

$$\sum_{i} \sum_{j} S_{ij} c_{ij} = known \ value$$

The model is run with starting values for the two parameters and we see what values of the statistics we get and then we change these towards better values and so on until we get the ones that meet these equations. I sent a couple of years of my life working on this problems in the early 1970s and to prove it

Google	he Calibration of Gravity, Entropy, and Related Models of Spatial Interaction 💌
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Articles Case law My library	The calibration of gravity, entropy, and related models of spatial interaction <u>M Batty</u> , S Mackie - Environment and Planning A, 1972 - epn.sagepub.com Abstract This paper presents a methodology for deriving best statistics for the calibration of spatial interaction models, and several procedures for finding best parameter values are described. The family of spatial interaction models due to Wilson is first outlined, and then some existing calibration methods are briefly reviewed. A procedure for deriving best
Any time Since 2017	statistics based on the principle of maximum-likelihood is then developed from the work of Cited by 177 Related articles All 6 versions Cite Save
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Ok that is probably enough for the first session – the next 50 minutes will be a demo of our singly constrained interaction model for E & W which is an online



#### Extensions & Applications Topic 2: Predicting the Impact of Large Scale Urban Infrastructures

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# Outline

- A Very Important Key Point to Begin With
- Scaling The Models: More Zones, More Detail
- Links to ABM (Agent-Based Models)
- A Quick Demo of QUANT
- Problems with the Models
- Setting and Testing Scenarios
- Big Infrastructure Projects: Crossrail, HS2, The Third London Airport
- Future Urban Models and Use in Planning

#### A Very Important Key Point to Begin With

The demand for various outputs in such integrated LUTI models is subject to capacity constraints. For example a model producing J to W flows –  $T_{ij}$  – is subject to the capacity of the network and also when we add up the number of workers getting to any place to live, this must be less than the density limit. We need to iterate. This is the killer – it has been like this since the beginning of these models

$$T_{ij} = E_{i} p_{ij} \sim E_{i} A_{j} \exp(-\beta c_{ij})$$

$$-if T_{ij} > C_{ij} then c_{ij} is increased, as c_{ij} = c_{ij} \frac{T_{ij}}{C_{ij}}$$

$$F_{j} = \sum_{i} T_{ij} = \sum_{i} E_{i} p_{ij}$$

$$F_{j} > Z_{j} then A_{j} is decreased, as A_{j} = A_{j} \frac{P_{j}}{Z_{j}}$$

$$F_{j} = \sum_{i} E_{i} p_{ij}$$

It is made even worse by the fact that the networks are at a different (finer) scale than the aggregated zonal model. When we change  $c_{ii}$  we need to drill down and look at individual elements

$$c_{ij} = c_{ij_1} + c_{j_1 j_2} + c_{j_2 j_3} + \dots + c_{jnj}$$

It may be that the one in the red box needs to be increased but this segment might be common to other trips and thus it is impossible to figure out which ones to increase and in what order. We thus risk setting other trips out of equilibrium, and thus no overall equilibrium can be guaranteed.

In fact if all we do is alter  $C_{ij}$  then we can be more certain that the model will converge but this may take many iterations.

If we have the simpler model where there is only one  $C_{ij}$ , then this is more likely to converge but for a very large model it might take many iterations

#### Scaling The Models

- We are building a model which is for the UK currently England and Wales – at the same level as our current urban models. Absolutely essential to do this because of wider interaction effects – the 'where does London begin and end' problem
- The model is web based any user can access it from anywhere – and in this sense, it has multiple users.
- It is fast to run many problems of map delivery from server to client and so on but these are being sorted. Biggest issue is with transport networks and their updating at a very fine scale
- The model is called QUANT a not very original title but easy on the eye so to speak – it means Quantitative Urban ANalytics forecasTing, or some variant thereof
- It grew out of a version of the model just demoed
- It is designed to let any informed expert develop scenarios

Let me show you the spatial representation first – what we call middle layer super output areas – MSOAs – which have around 7000 persons per unit on average

There are some 52 million persons in E and W in 2011; there are some 27 million jobs; there are 7201 MSOAs

Why E and W and not Scotland or NI





We could build this at the finest geographical scale – it would take ages to run because our matrices would be of the order 181K<sup>2</sup> and then we would have to move to ABM ~ 150 p p zone

#### Links to ABM: Where Are We

• Its looks like as we spatially disaggregate to the kind of data we are now getting we can begin to think about ABM – modelling every individual – so our equations might look more like this

 $p_{ij} \sim E_i A_j \exp(-\beta c_{ij})$  is the probability that

an individual working in i will reside in j

- We could simply take the maximum probability for each individual travelling to 7200 other zones and if each of the individuals was in a slightly different place in the zone – which we might know from address point data – we would get a variation around the aggregate solution.
- If more variables were different and we knew their mode of travel etc and income and so on we would have a much richer set of probabilities to work with. In QUANT and our previous models we do have three modes of travel in fact – rail, road, bus

- In fact this is the way to thinking of the model in individual terms and using Monte Carlo simulation we can generate an individual from an aggregate model very easily if we had a big enough computer which we don't have yet and cannot justify.
- The model would be pretty simple anyway and it is only 'just about' agent-based in that the individuals are not influenced by the behaviour of other individuals other than through the aggregate variables that pertain to other agents
- However it is when we begin to iterate a large model such as the one we have that things get really complicated and we need to formulate the way the model allocates activity in an agent-based sense.
- So to summarise, the way to building an agent-based version which is much richer is clear but the computation is horrendous. We also have a sense in which the model users are agents and this opens up an entirely different Pandora's box which I wont discuss here but it is of great interest. But before all this, let me give you a quick run of what the model does.

## A Quick Demo of QUANT

- Here is the web site that you can explore caveat emptor it's a prototype, its free, it is an alpha version not even beta
- <u>http://quant.casa.ucl.ac.uk</u>
- Its is based on a simple structure of letting the user explore the data, then run the model (and calibrate it although as this happens every time it like an initiation of variables), then the user can look at the model outputs (predictions of the observed cross section) and finally set up scenarios – currently changes in employment and changes in rail lines – due to our (the UK Govts) current obsession with infrastructure projects
- Many issues here that are not reported to do with computational and programming considerations
- Visualisation to date is quite primitive.
































### **Problems with the Models**

The problem we have with getting the model to reach an equilibrium with respect to the supply of transport through the capacity of the network is that such an equilibrium is continually disturbed by the fact that the networks are at much more detailed scale

We need to assign trips to the networks and due the fact that they compete for network space, we cannot change travel costs in a simple way. To an extent this is the problem faced in MATSIMs – the ABM/Microsimulation model developed out of TRANSIMs which we are running also for London. It take four days to converge as the trips keep on disturbing those that have been predicted.

Some versions of these models have simply developed a separate transport model alongside and accepted that the urban model produces generic interactions not trips. But this is a fudge. Let me show the complexity of the networks underlying the model



If we work out the surplus trips that cannot be loaded onto the network which are

 $S_{ij} = (T_{ij} - C_{ij})$ 

we can then allocate them differently, one at time as though they are agents.

We are experimenting with doing this – and so in essence we are making use of the aggregate model to allocate demand to meet supply and the surplus demand is then allocated using an ABM – or rather it is allocated for disaggregates – to the individual level where the supply constraints are reached incrementally

Yes it is a fudge, No it isn't an agent based model I hear you say.

But it is on the way and the logical outcome of proceeding in this direction is an ABM and probably like in our MATSIM model, would be based on a sample of employment – a 10% sample would be some 2.7 million employees

We think this is currently feasible. Ok let me show you some runs of the model and the I will wrap up

## **Setting Up and Testing Scenarios**















## Big Infrastructure Projects: Crossrail, HS2, The Third London Airport:

Again I could spend a long time on these applications and all I can do here is show what is now possible – it is possible to test different alternatives over and over again. And any of us can do it – all you need a bit of training in the models – I suppose planning education should do this – but that is another story and not one for this evening

I will first show Crossrail and the HS2 because the impacts are much much wider than many of models can show. This reveals how important it is to make our model bigger spatial and to capture the widest economic benefits we can identify. And lastly I will deal with the Third Runway

# Crossrail

Reading, Heathrow, Shenfield, Abbey Wood





Lectures on Urban Modelling

## Crossrail Number of Improved Journeys (n<sub>i</sub>)



## Crossrail Population change (rail mode only)



## Crossrail Population Change (all modes)







## HS2 Route Maps





## High Speed 2 Population change (all modes)



### 276 Evaluation in the Planning Process





CHAPTER 11

### A Major Project: Third London Airport

(June 1968-December 1970)

The deliberations of the Roskill Commission on the Third London Airport were distinguished by the very clear and logical process by which recommendations were arrived at. The Commission adopted five cycles, from the definition of a "universe" of possibilities to a short-list of four sites, and then directly to a recommended alternative. One particularly important feature was that the evaluation criteria were determined at the outset of the process and were then used consistently throughout.

#### 11.1. BACKGROUND

The eventual recommendation by the Roskill Commission of Cublington as the site for the Third London Airport in preference to Foulness ted to considerable controversy. This controversy, coupled with the fact that the Government eventually decided in favour of Foulness against the Commission's recommendation, has obscured many interesting and original features of the process by which the Commission reached its recommendation. In this chapter we discuss some of the main features of this process. It does not cover the ground of the many critiques of the Commission's work which have mainly concentrated on the treatment of measured items in the Commission's Research Team's evaluation; intangibles in the decision; important issues affected by the decision but outside the Study terms of reference, and on the validity of the Commission's conclusion. In this chapter any reference to these topics is restricted to those cases illustrating a feature of the site selection process itself.

One might say that the setting up of the Commission was a result of public outcry over an inadequate process of site selection. The arguments against the decision to locate the airport at Stansted were largely motivated, and strongly supported, by the fact that the Stansted decision was not shown to be in the general public interest. There was no formal evidence to suggest that the alternative possible sites to Stansted which were considered had been rigorously investigated, with all factors for and against them, in comparison with Stansted, taken into account in the decision. Much of the work behind the selection of Stansted was undertaken in

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The Objectives Used by the Davies Commission in Assessing the Various Options for the Expansion of Heathrow and/or Gatwick

Sift criteria categories	Appraisal objective
Cost	To make efficient use of public funds, where they are required, and ensure that the benefits of schemes clearly outweigh the costs, taking account of social, environmental and economic costs and benefits.
Delivery	To be affordable and financeable, including any public expenditure that may be required and taking account of the needs of airport users.
	To have the equivalent overall capacity of one new runway operational by 2030.
	To actively engage local groups in scheme progression, design and management.
Operational Viability	To enhance individual airport and airports system resilience.

### Table 4.1: The Commission's Appraisal Framework objectives

Sift criteria categories	Appraisal objective
Strategic Fit	To provide additional capacity that facilitates connectivity in line with the assessment of need,
	To improve the experience of passengers and other users of aviation.
	To maximise the benefits of competition to aviation users and the broader economy.
	To maximise benefits in line with relevant long-term strategies for economic and spatial development.
Economy	To maximise economic benefits and support the competitiveness of the UK economy.
	To promote employment and economic growth in the local area and surrounding region.
	To produce positive outcomes for local communities and the local economy from any surface access that may be required to support the proposal.
Surface Access	To maximise the number of passengers and workforce accessing the airport via sustainable modes of transport.
	To accommodate the needs of other users of transport networks, such as commuters, intercity travellers and freight.
	To enable access to the airport from a wide catchment area.
Environment	To minimise and where possible reduce noise impacts.
	To improve air quality consistent with EU standards and local planning policy requirements.
	To protect and maintain natural habitats and biodiversity,
	To minimise carbon emissions in airport construction and operation.
	To protect the quality of surface and ground waters, use water resources efficiently and minimise flood risk.
	To minimise impacts on existing landscape character and heritage assets.
	To identify and mitigate any other significant environmental impacts.
People	To maintain and where possible improve the quality of life for local residents and the wider population.
	To manage and reduce the effects of housing loss on local communities.
	To reduce or avoid disproportionate impacts on any social group.

Lectures on Urban Modelling








We have Tested the Impact of the Third Runway on E&W in terms of Where the Population from an Extra 50000 Jobs will Locate



## Future Urban Models and Use in Planning

- We need a new way of thinking about science in public policy
- It needs to inform, it must be based on conditional prediction – what if scenarios
- It needs to accept the inherent unpredictability of complex systems and this suggest continual action

   this is little different from what has always been preached in urban planning – continual review, but the cycles need to be faster
- We must be aware that the systems we are dealing with moving targets of increasing complexity

## Where I am

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