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Distinguished Lecture Series

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תשע"ד

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Visualising Spatial Complexity

Rank Size, Scaling, and Space-Time Dynamics

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http://www.ComplexCity.info/

http://www.casa.ucl.ac.uk/

http://www.spatialcomplexity.info/files/2014/03/BATTY-TECHNION2.pdf

Outline

- City-Size Distributions: Scaling and the Rank-Size Rule
- Macro-Stability & Micro-Volatility
- The Rank Clock and Other Visual Mnemonics
- Classic Exemplars
    - US City Populations 1790-2000
    - Skyscrapers
- US Metro Area Populations
- Japanese Populations
- Firm Sizes
- Adding Place to Rank Clocks:
- Animations: Rank Clocks and Rank Space
- Next Steps

The key thesis – we need to visualise dynamic systems where the system appears stable at the macro level but volatile at the micro – there are two nice quotes to start

"I will [tell] the story as I go along of small cities no less than of great. Most of those which were great once are small today; and those which in my own lifetime have grown to greatness, were small enough in the old days"

From **Herodotus – The Histories** –
Quoted in the frontispiece by Jane Jacobs (1969)
The Economy of Cities, Vintage Books, New York

But cities have a remarkable degree of regularity and stability with respect to their size …

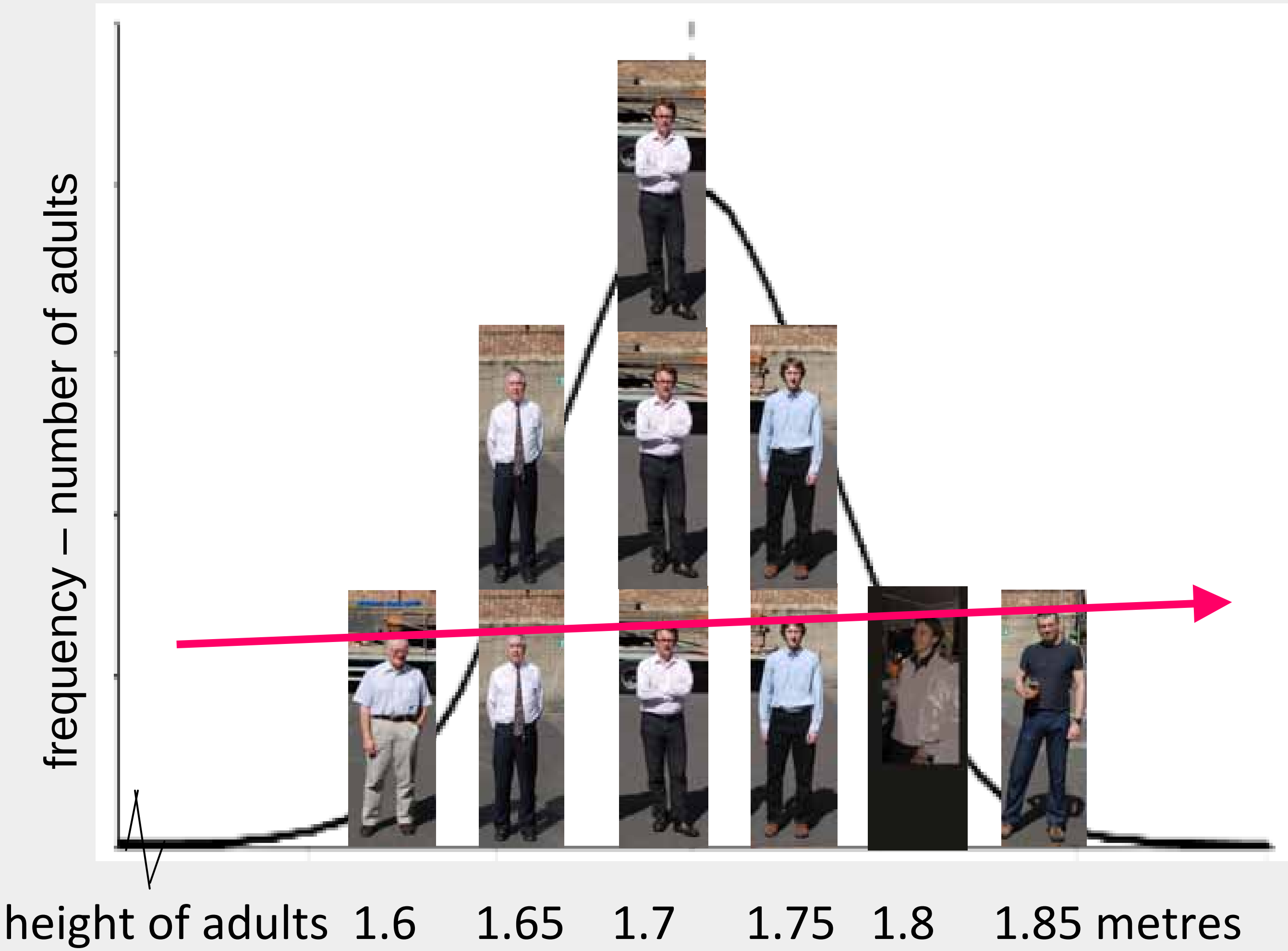
"The size distribution of cities in the United States is startlingly well described by a simple power law: the number of cities whose population exceeds P is proportional to 1/P. This simple regularity is puzzling; even more puzzling is the fact that it has apparently remained true for at least the past century."

Paul Krugman, 1996, Confronting the Mystery of Urban Hierarchy, **Journal of the Japanese and International Economies 10**, 399–418.

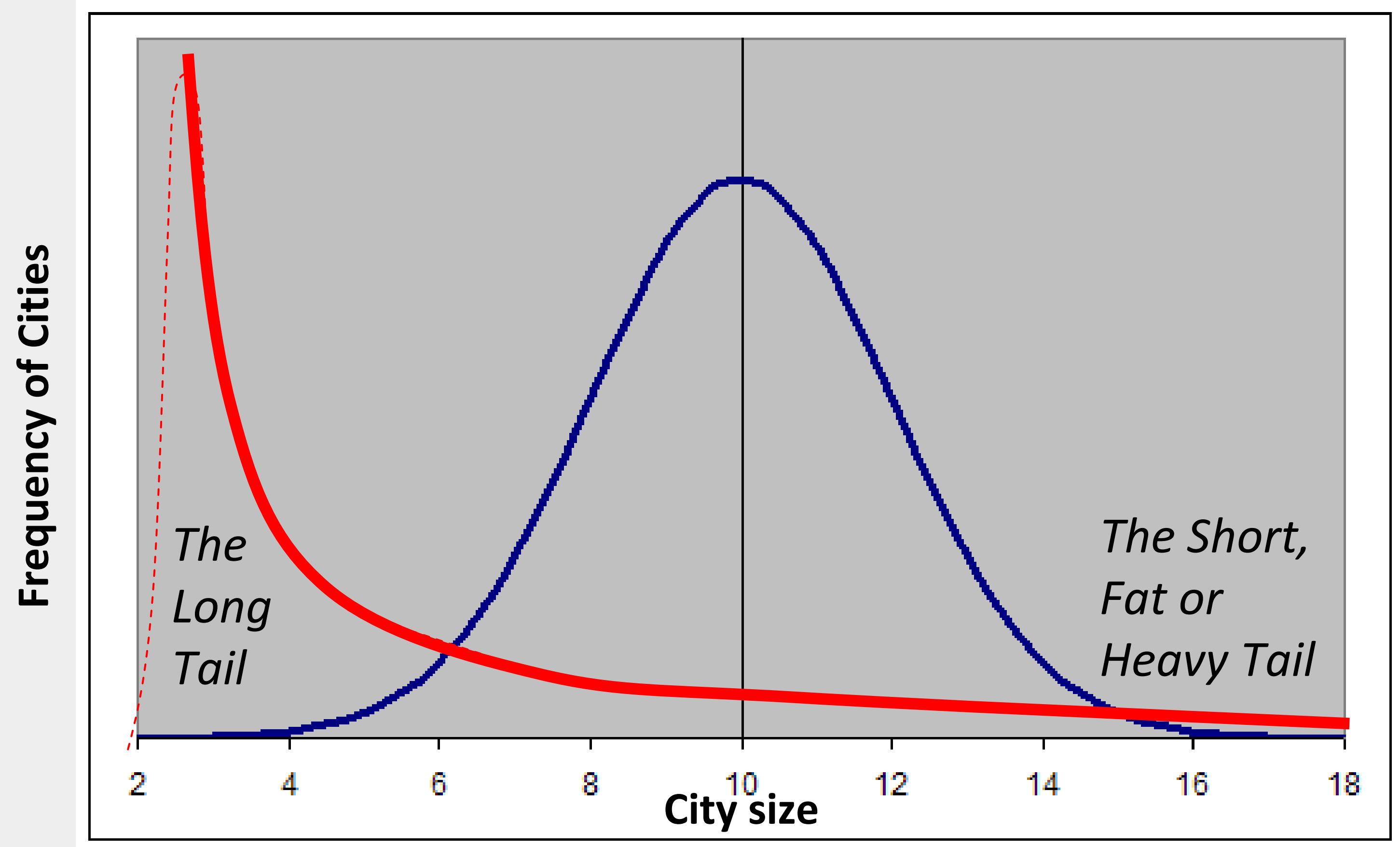
City-Size Distributions: Scaling and the Rank-Size Rule

Let us look at a group of people all of different heights

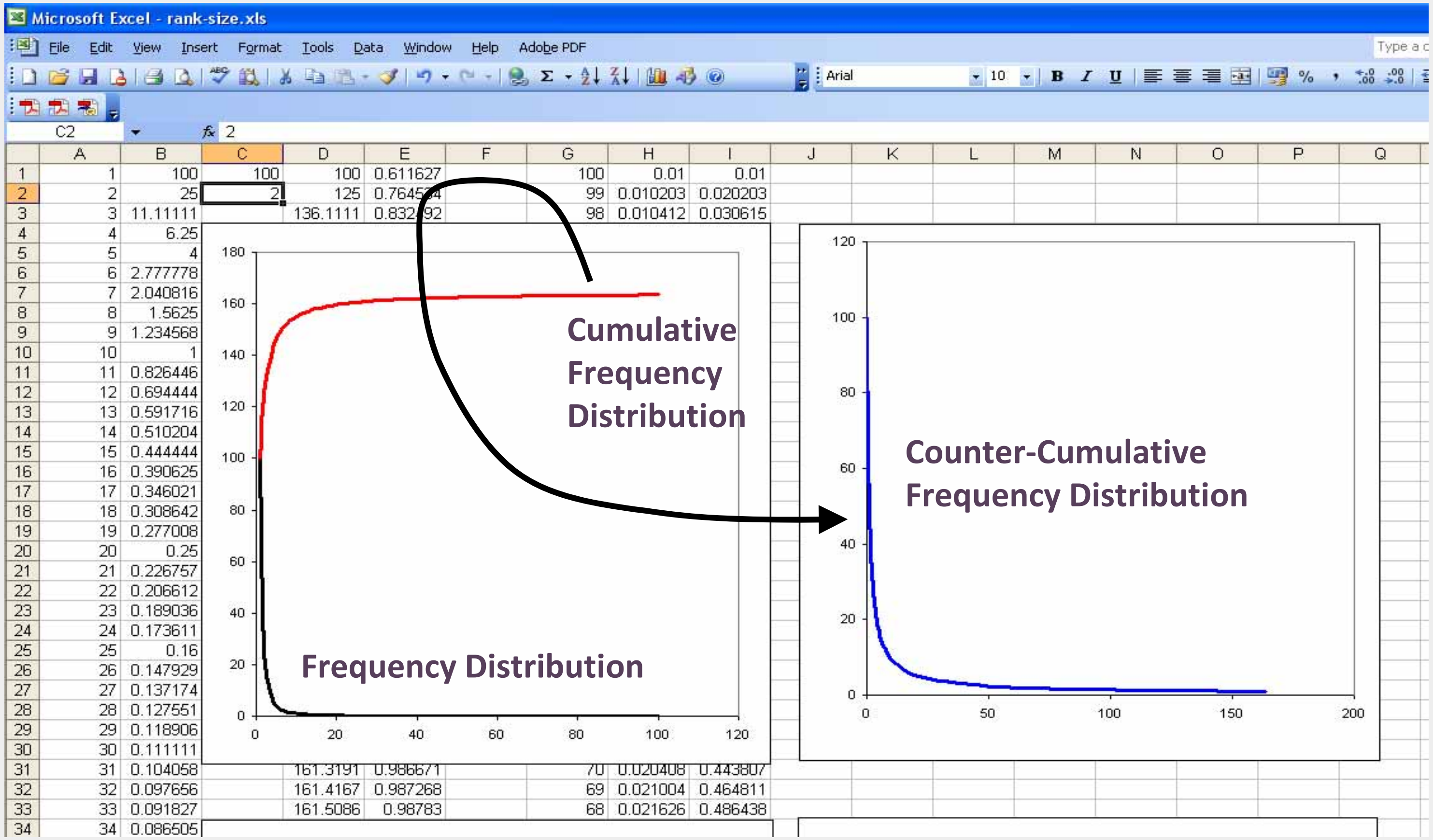
Mike *Rui* *Andy* *Richard* *Duncan* *Phil*


frequency – number of adults
height of adults 1.6 1.65 1.7 1.75 1.8 1.85 metres

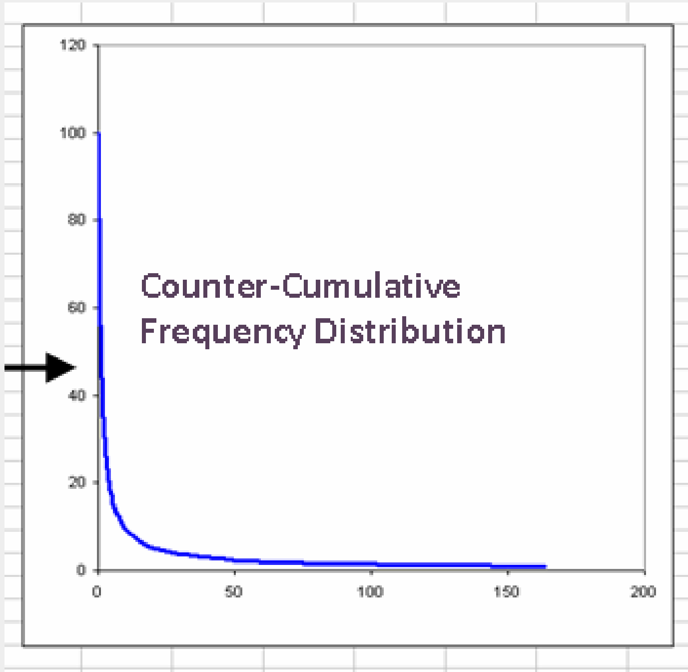
When we look at things like city sizes, we do not find a normal distribution but we find something that is like a power law or at least a lognormal

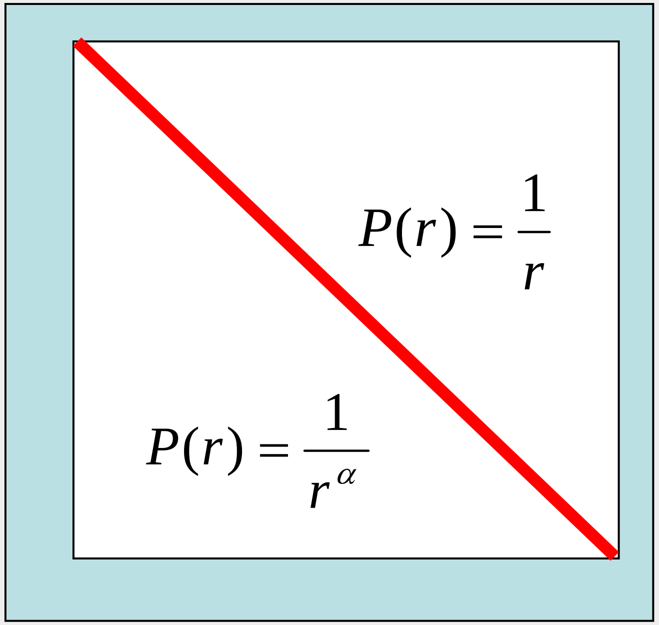


I am going to spare you the algebra although it is easy and this is how we get the rank size distribution from the frequency power



Now if we take logs – i.e. a simple transformation, this power law becomes a straight line in 2-d space and it is this form that we refer to as the rank-size rule





Macro-Stability & Micro-Volatility

Essentially we can illustrate the stability of city size population by showing how this rank size curve changes over time

It remains quite stable for the US from 1790 to 1930 and this is what Zipf, amongst others, discovered in the 1930s. And it prompted the Krugman quote.

It is all in Zipf's famous book. And Paul Krugman in the late 1990s also said that Zipf's Law and Pareto's Law before, are the only real examples of iron laws in the social sciences. Let us see what he meant.

The Rank Clock and Other Visual Mnemonics

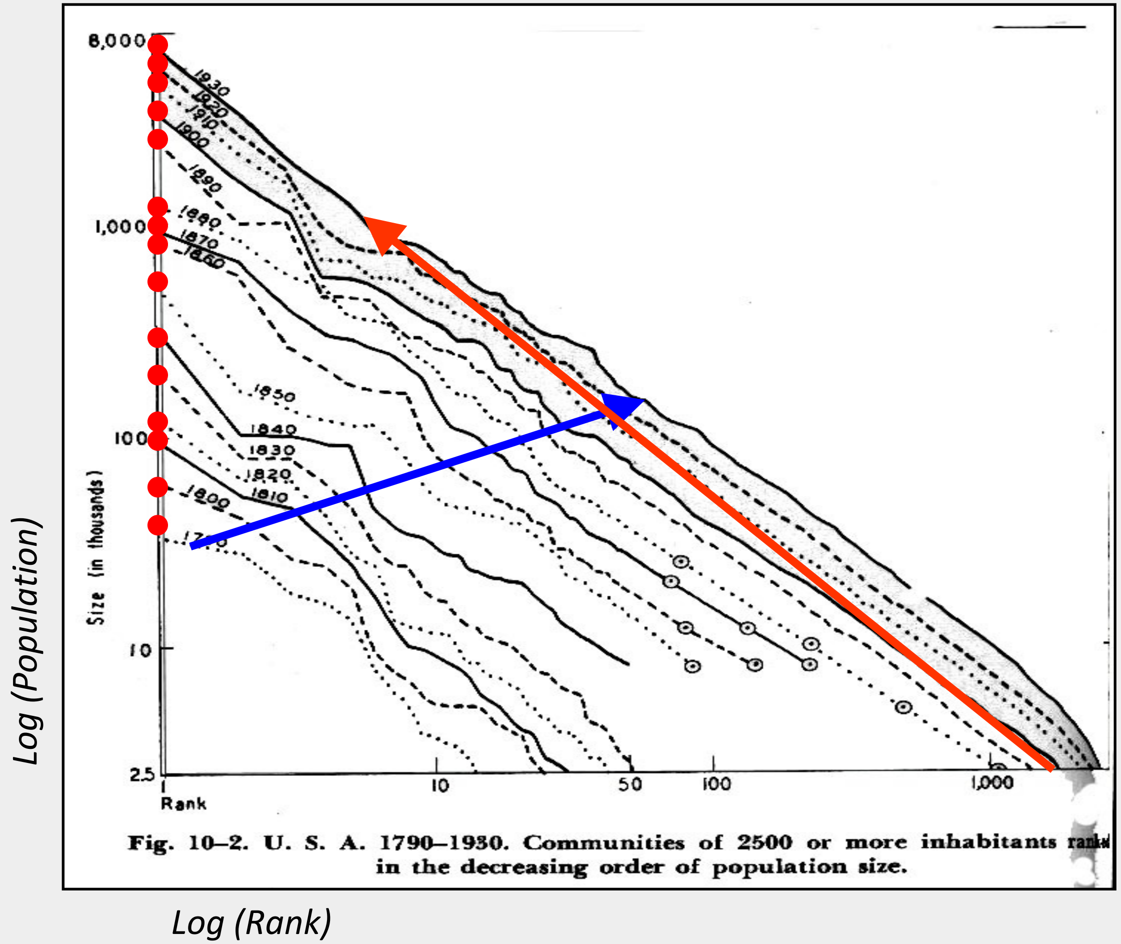


Fig. 10–2. U. S. A. 1790–1930. Communities of 2500 or more inhabitants ranked in the decreasing order of population size.

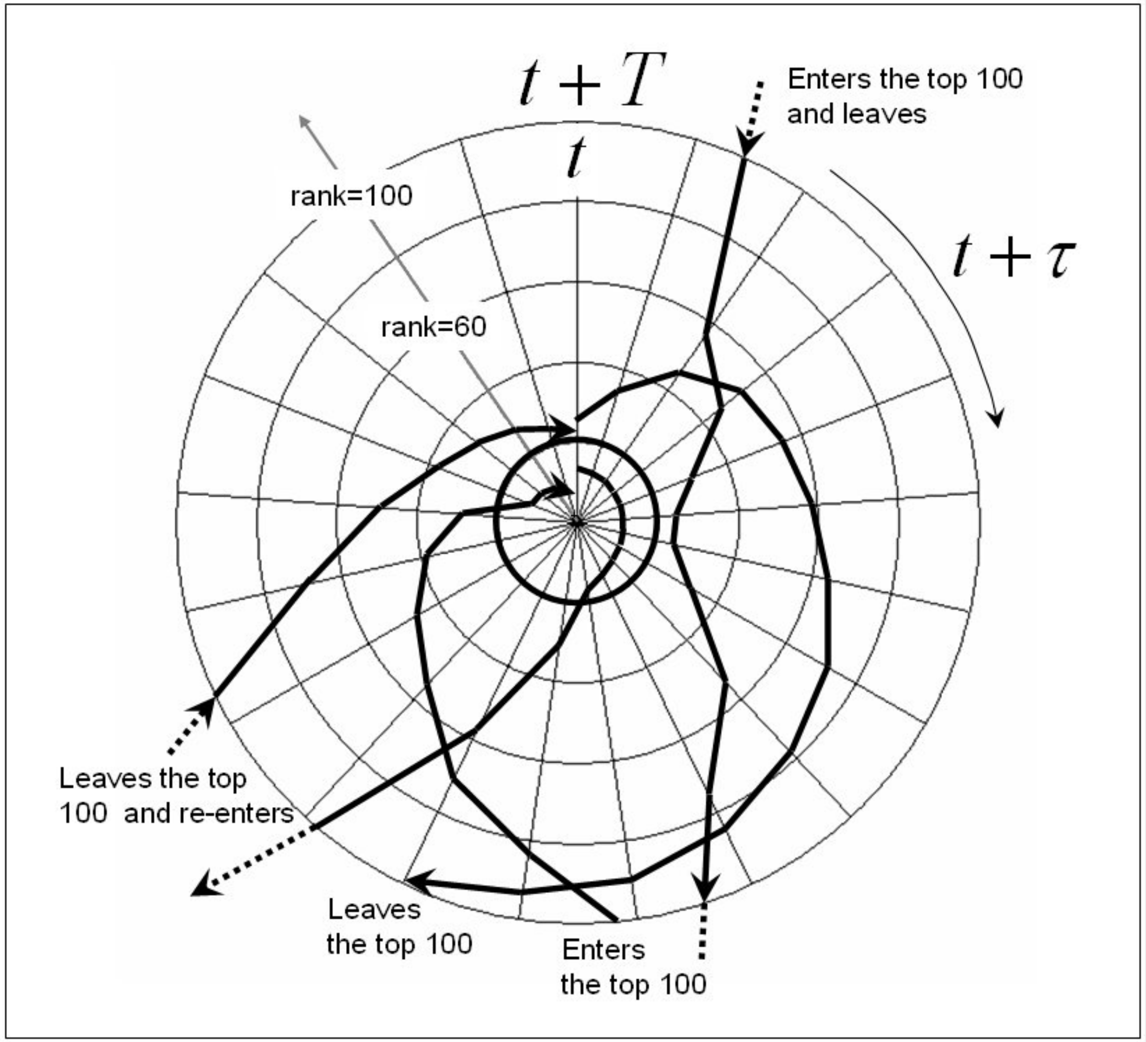
From George Kingsley Zipf (1949) ***Human Behavior and the Principle of Least Effort*** (Addison-Wesley, Cambridge, MA)

The idea of the rank clock is to discard population because rank is its equivalent and just plot changes in rank with respect to time

We can do this in rank space but it is not as effective as in polar coordinate space

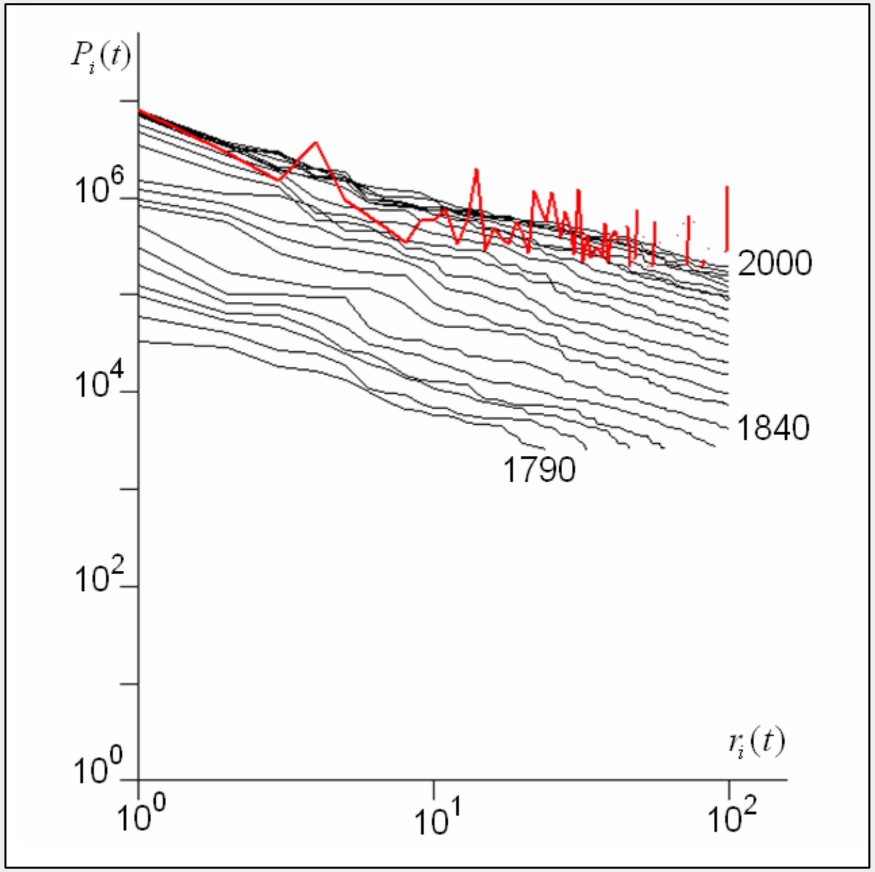
Here is an example of the possible trajectories of cities on the clock and we will stick with our US cities example for a bit longer, showing various possible plots and animations

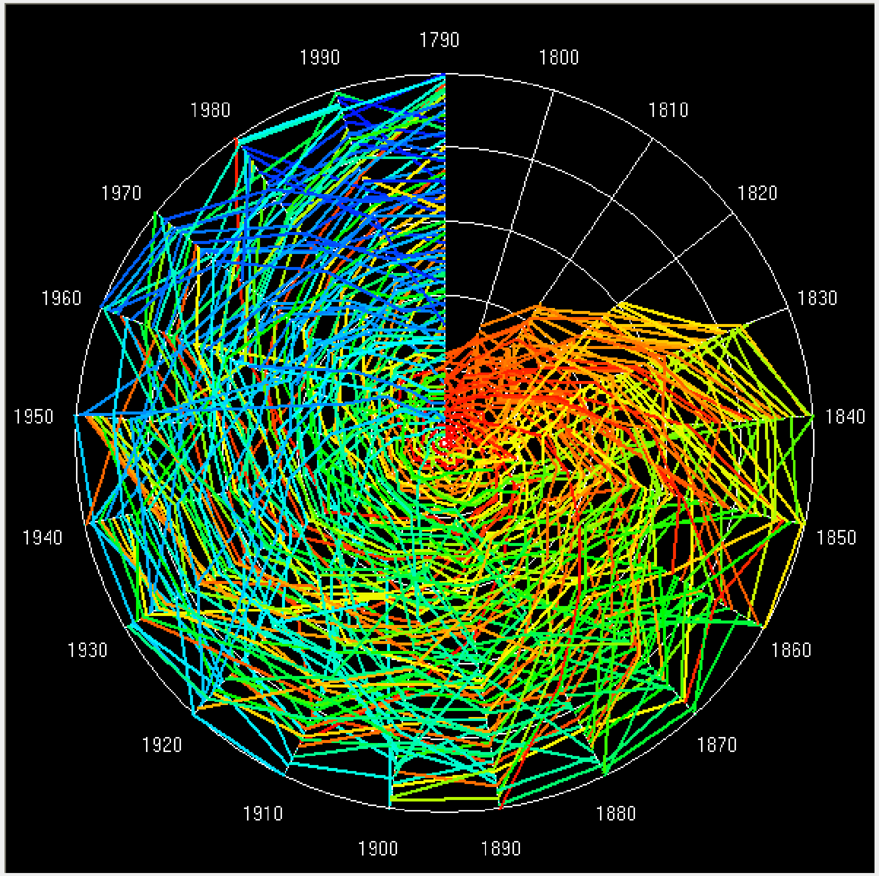
……….



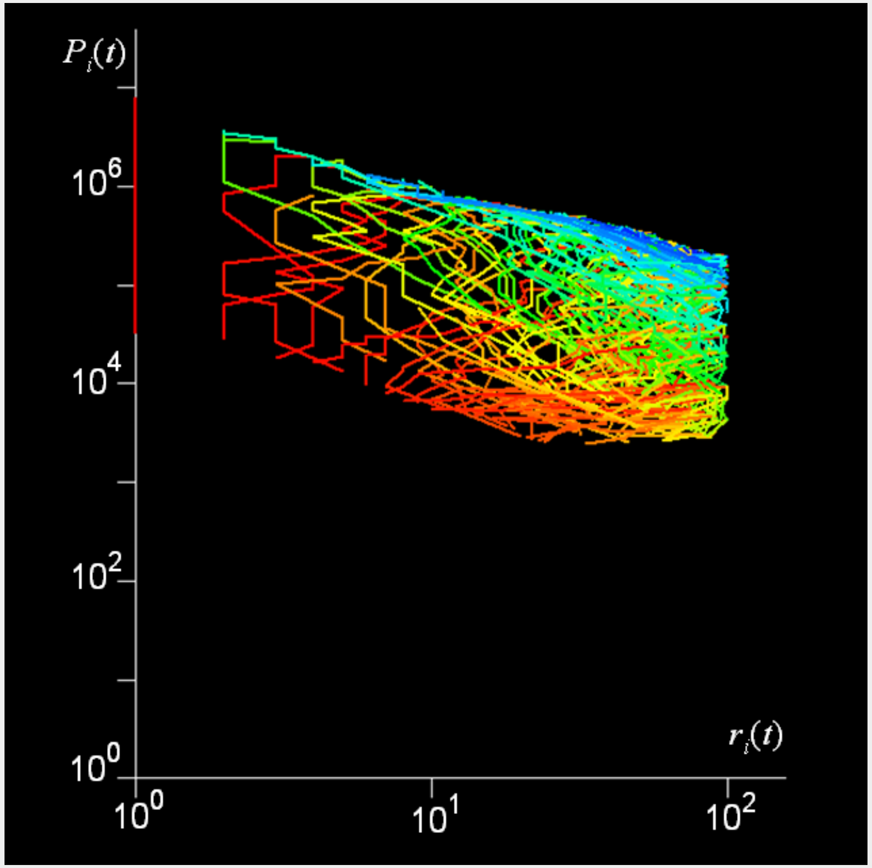
The Idea of a Rank Clock –rank is from number 1 at centre to 100 at edge and time goes in years in the usual clockwise direction

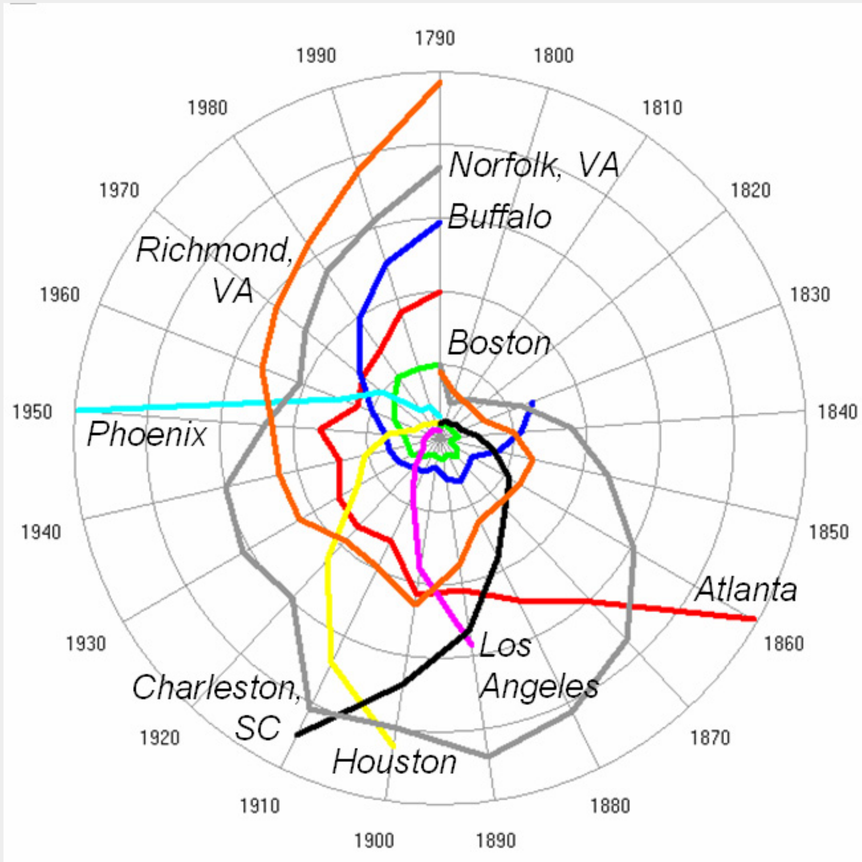
Classic Exemplars: US City Populations 1790-2000



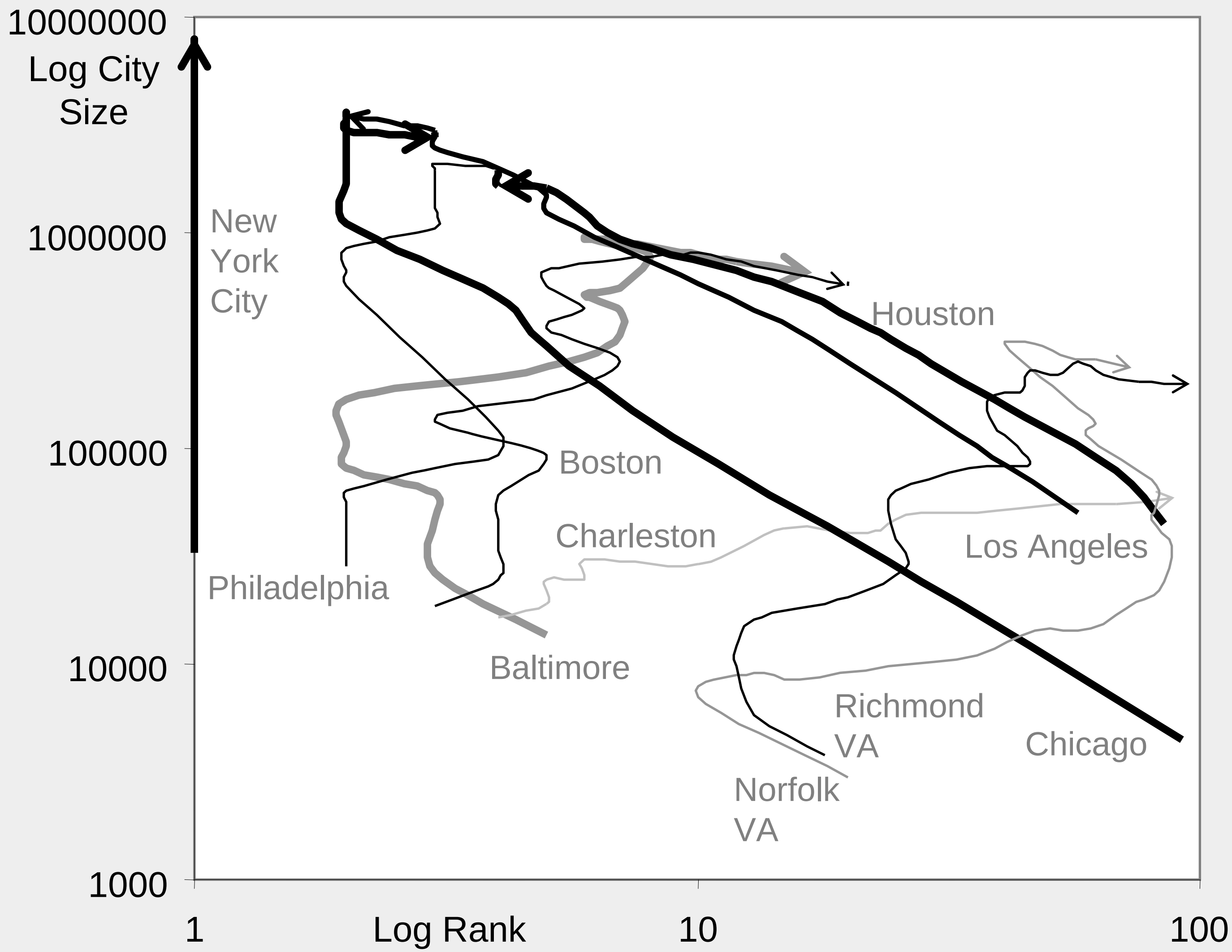


The ‘morphology’ of the clock should tell us something – i.e. the increase in cities, the volatility of ranks and so on.



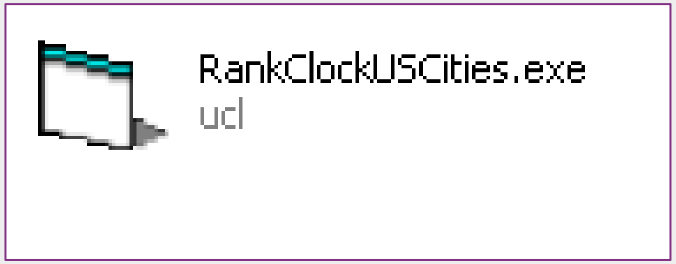


The rudimentary software for this in on our web site at
http://www.casa.ucl.ac.uk/software/rank.asp


10000000
Log City
Size
1000000
100000
10000
1000
New
York
City
Houston
Boston
Charleston
Los Angeles
Philadelphia
Baltimore
Richmond
VA
Chicago
Norfolk
VA
1
Log Rank
10
100

I will show you an animation of the clock but for a long while I simply plotted the clock and left it at that and measured various properties of the dynamics – but two years ago year we decided to animate it and of course the work that Ollie O'Brien and Martin Austwick, my colleagues are doing comes, from the notion that our graphics need to be livened up, brought alive and that we need to produce much more powerful explorations of the data

Here is the US city ranks from my desktop software



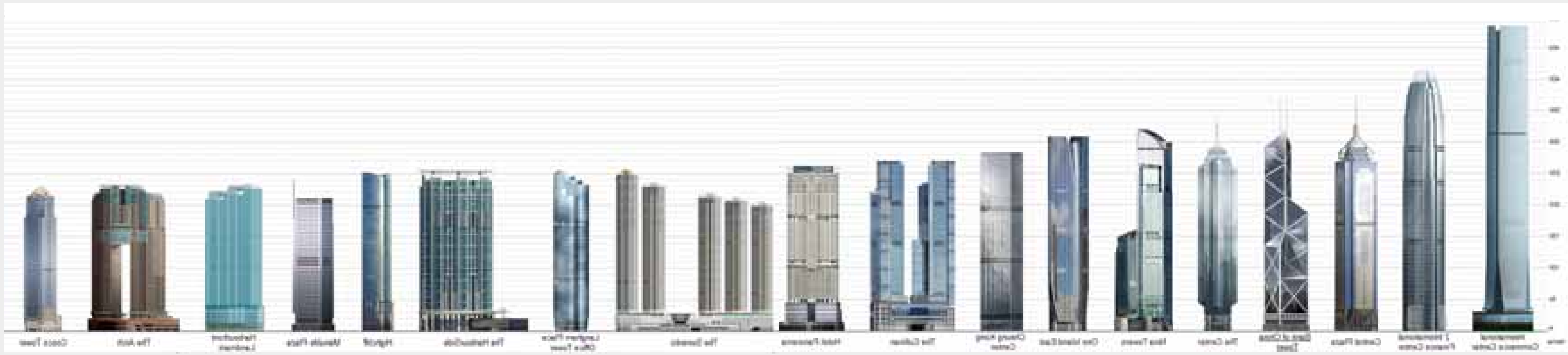
Classic Exemplars: Skyscrapers: High Buildings from 1900 or so in New York City and the World

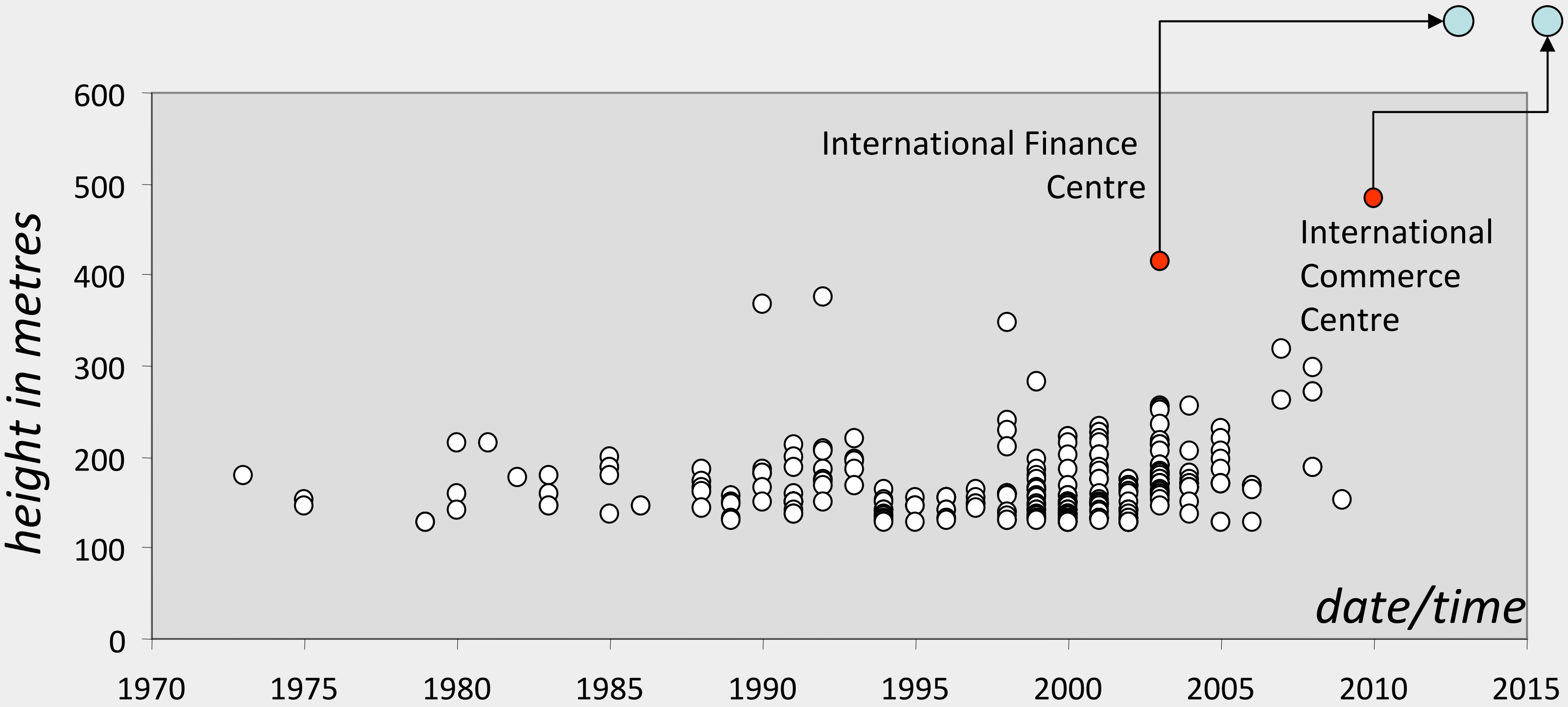
Cities grow and decline in size, the built environment is much more inert and discontinuous; and parts of it high buildings barely change other than their construction and subsequent demolition. Most of the world's skyscrapers, for example, (buildings higher than 20 stories, say) remain in place in terms of those constructed over the last century,

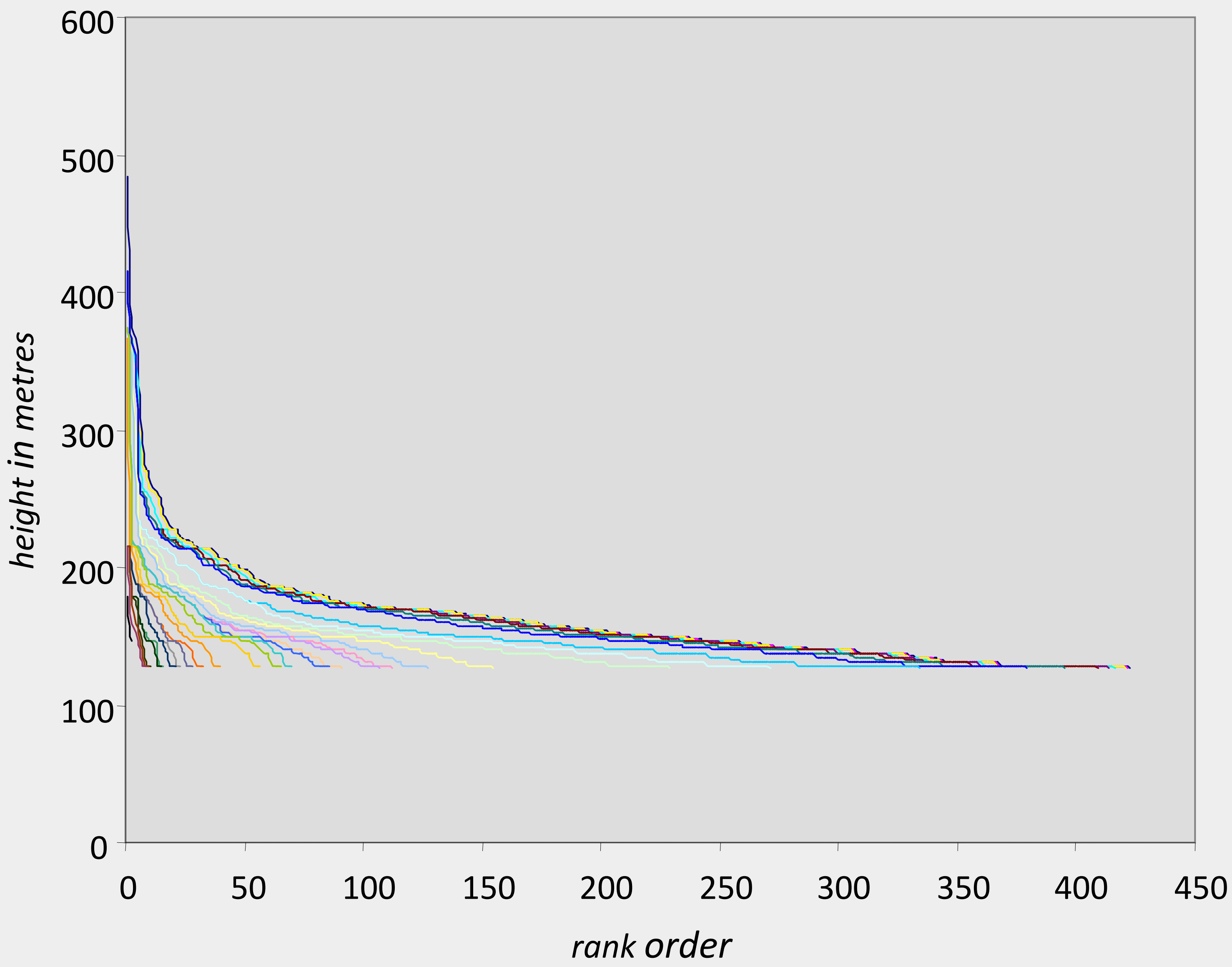
So their dynamics is likely to be different, very different. But there macro dynamics follows stable power laws too, so it seems. Let us look at Hong Kong

W Kowloon Corridor
西九龍走廊
King's Park
京士柏
Chatham Rd N
Princess
Hung Hom
紅磡
Hung Hom Bypass
Canton Rd
Kowloon Park
九龍公園
Tsim Sha Tsui
尖沙咀
Salisbury Rd
Cross Harbour Tunnel
W Kowloon Hwy (Toll rd)
西九龍公路
Sheung Wan
上環
Mid-levels
半山區
Central
中環
Harcourt Rd
Wan Chai
Wan Chai District
灣仔區
Causeway Bay
銅鑼灣
東區走廊
Caroline Hill
Morrison Hill
Leighton Hill
2000 ft
1 km
©2009 Google

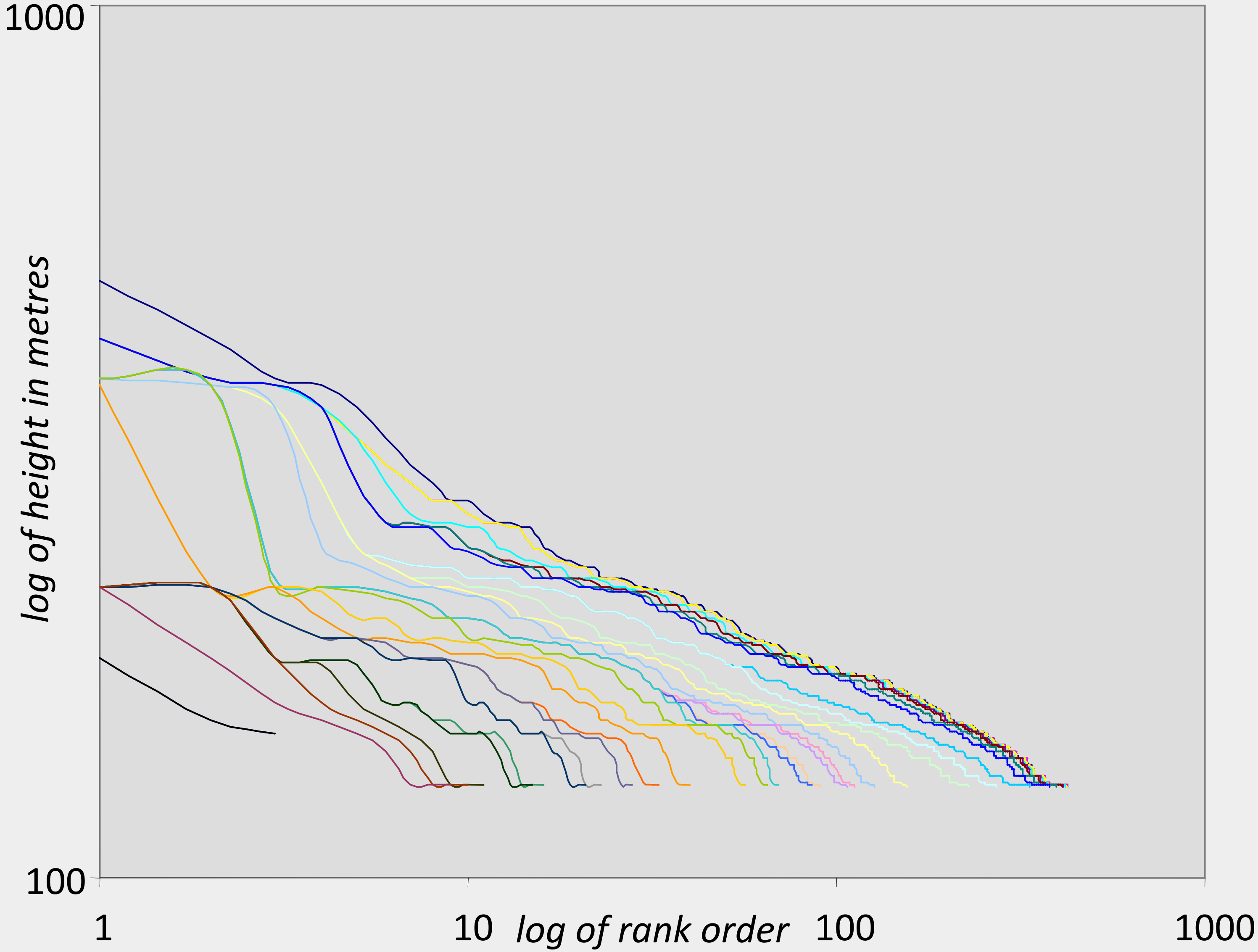
Hong Kong: The Dynamics of Tall Buildings

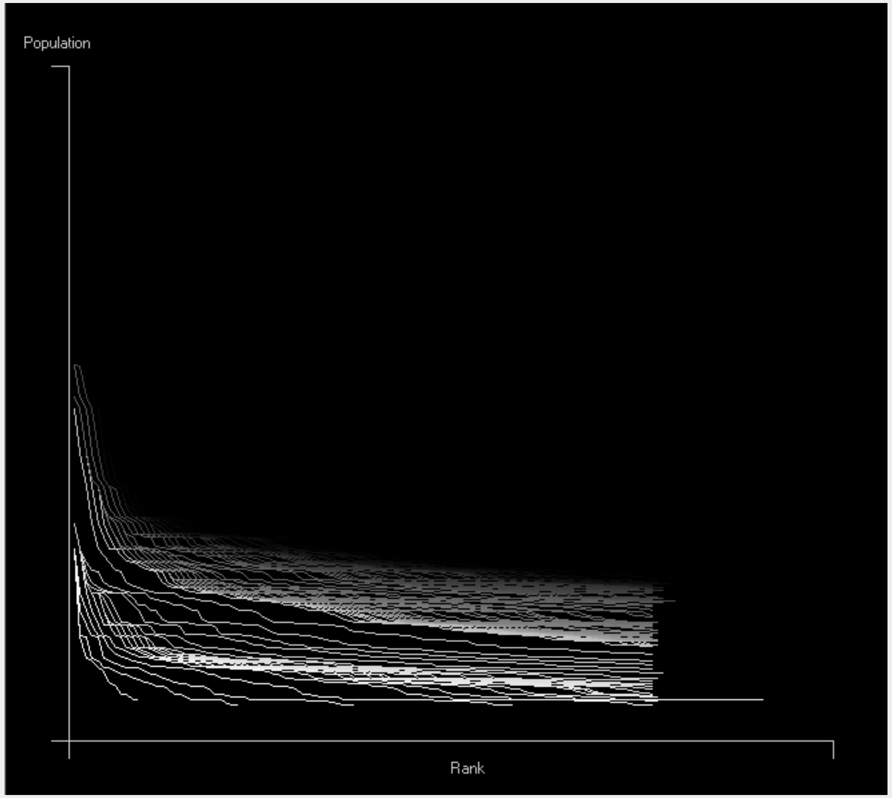


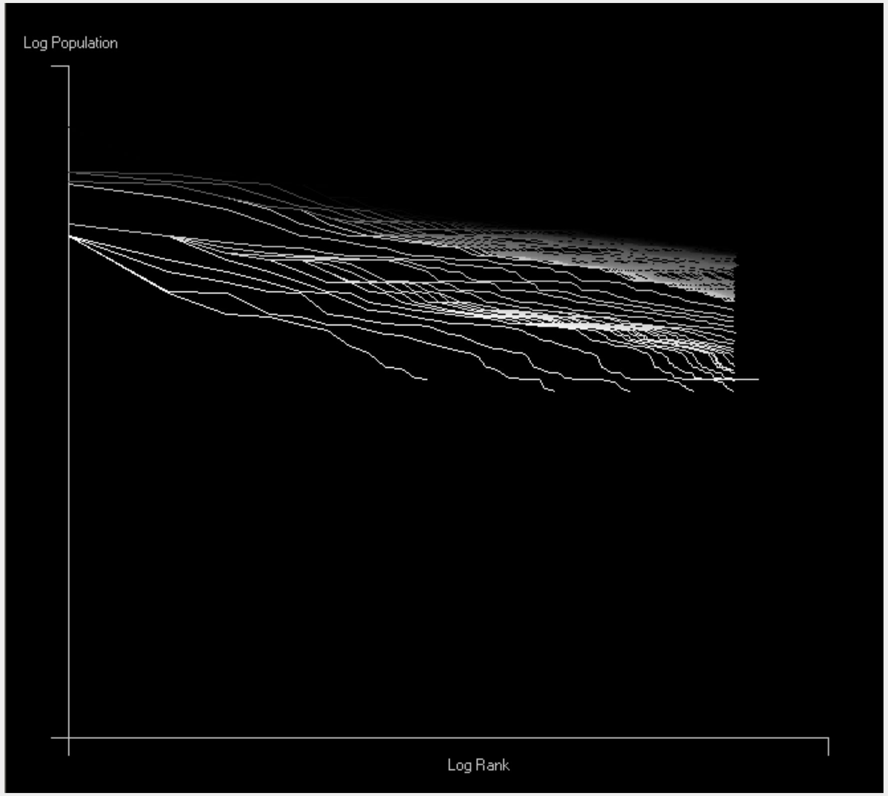




600
500
400
300
200
100
0
height in metres
0
50
100
150
200
250
300
350
400
450
rank order


1000
100
log of height in metres
1
10
log of rank order
100
1000

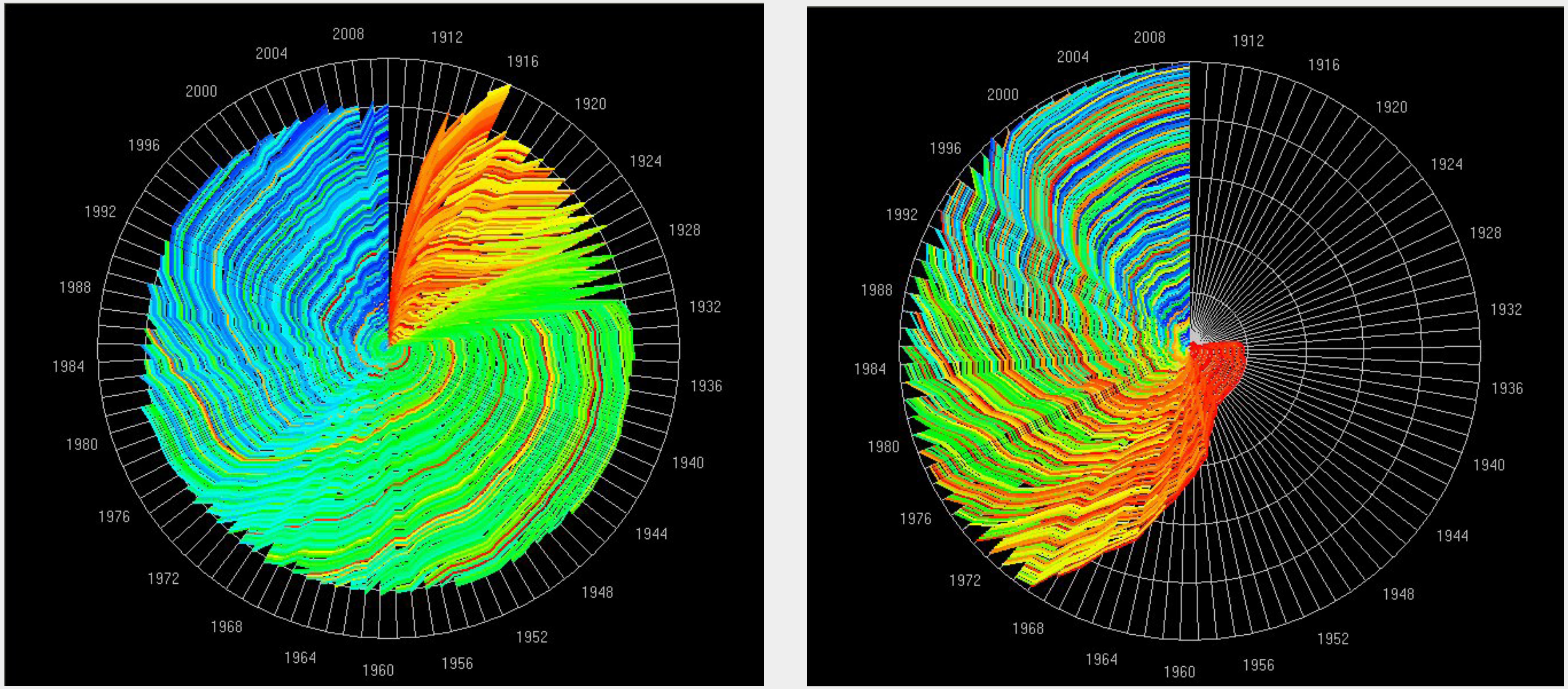




Rank Size Relations for the Top 100 High Buildings in the New York City from 1909 until 2010

power form (left), log form (right)

& here is the clock



Rank Clocks of the Top 100 High Buildings in the New York City (a) and the World (b) from 1909 until 2010

There is much more work to do on all this and I am only giving you a taste of this, now back to shape and size

US Metro Area Populations

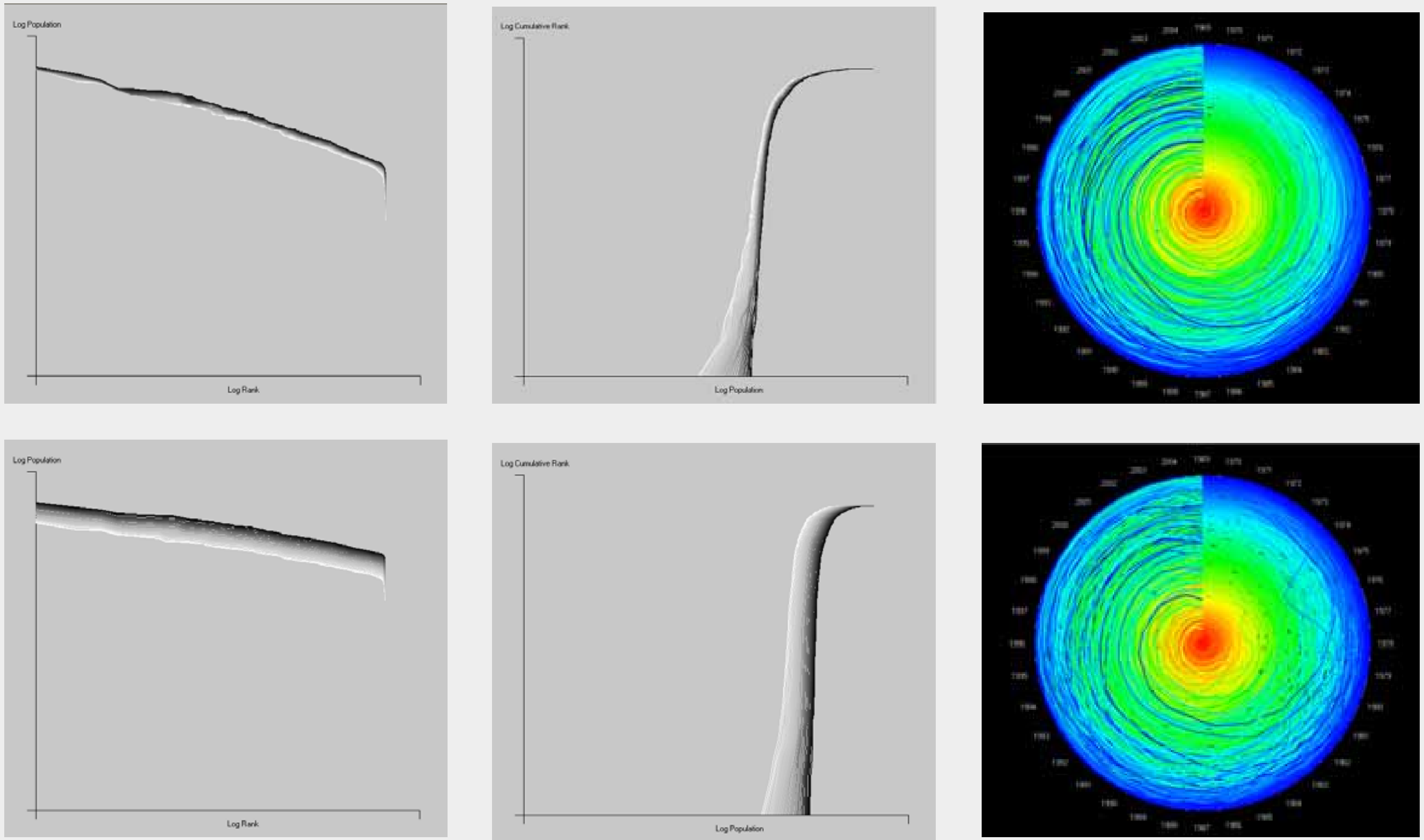
My last example – and we have many now – is from the US Bureau of Economic Analysis on metro areas –SMSAs from which I simply took their 366 regions for which population and income data are available for 37 years from 1969 to 2005.

One of the nice things here is that we can plot population ranks etc and income ranks – but we can also look at the ratio – population per capita which is much more volatile than each of the prime variables – let us see

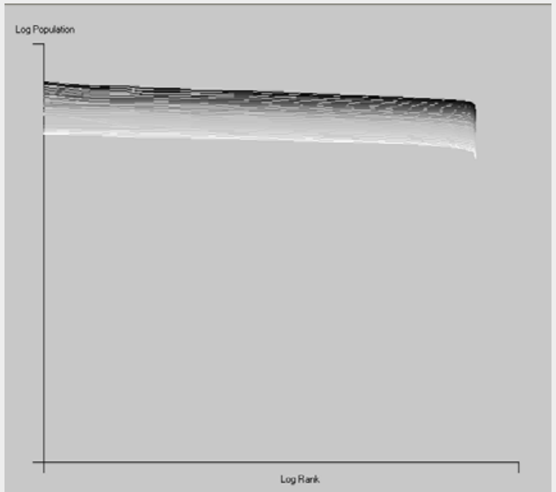
We can easily plot the shifts, spaces, and clocks for these population and income data. These follow very regular scaling laws, at least in their fat tails.

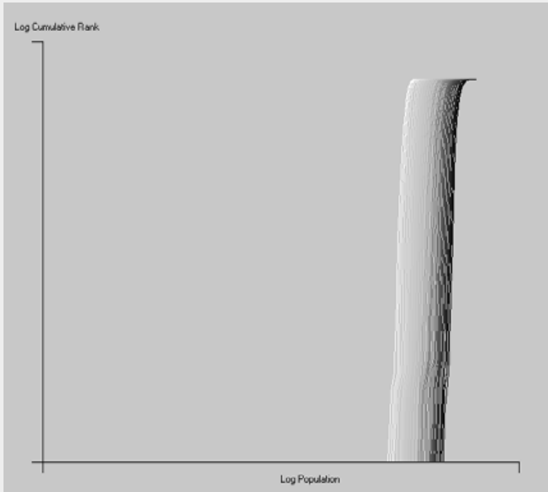
Population

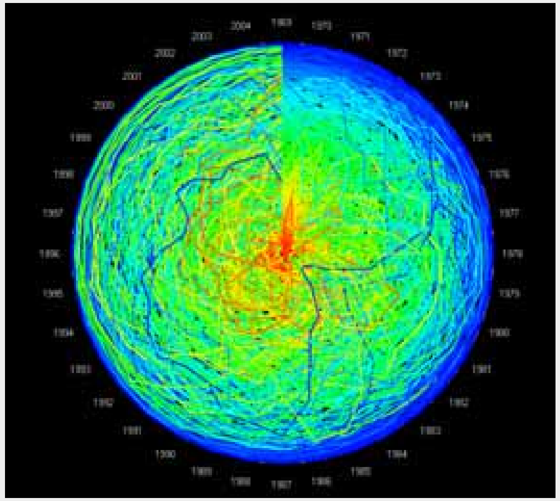
Income



But the real interest is in per capita income/wages – i.e. *Incomes / Population*. How does this rank? And if there are big shifts in rank, this shows divergence of these two variables







As you might expect the rank clock provides a graphic animation of this relative disorder at the micro level

Japanese Populations: Cities at Different Scales

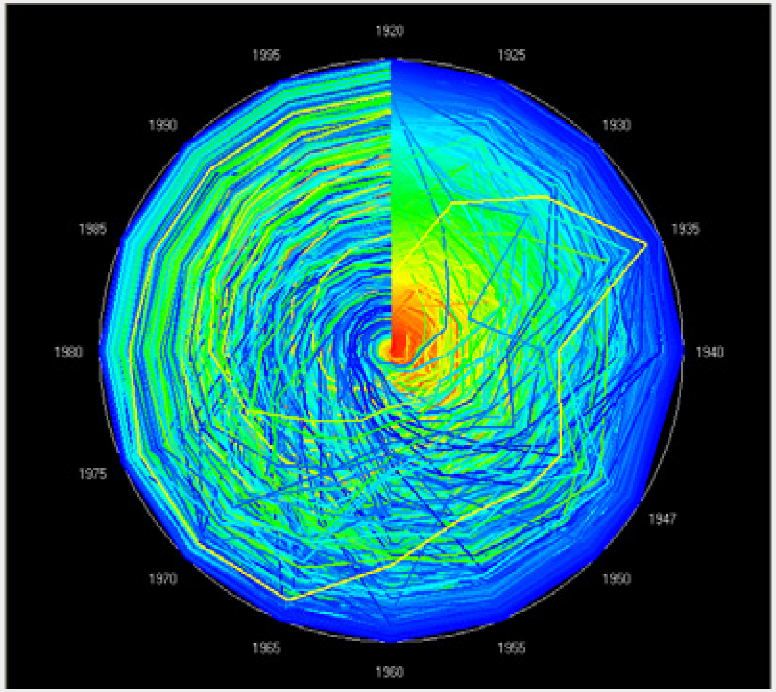
We have a large population data set of 2137 'cities' in Japan that are mutually exclusive subdivisions of the Japanese space and these are not cities in the sense of the US cities we have used.

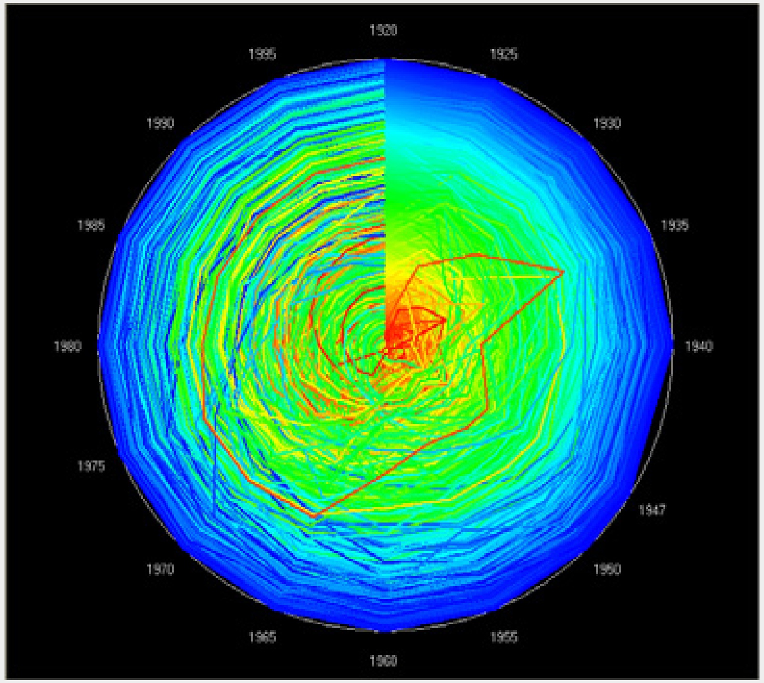
We also have an aggregation into 269 cities at a higher level

We also have other attributes of these cities – with data – such as area so we can compute densities

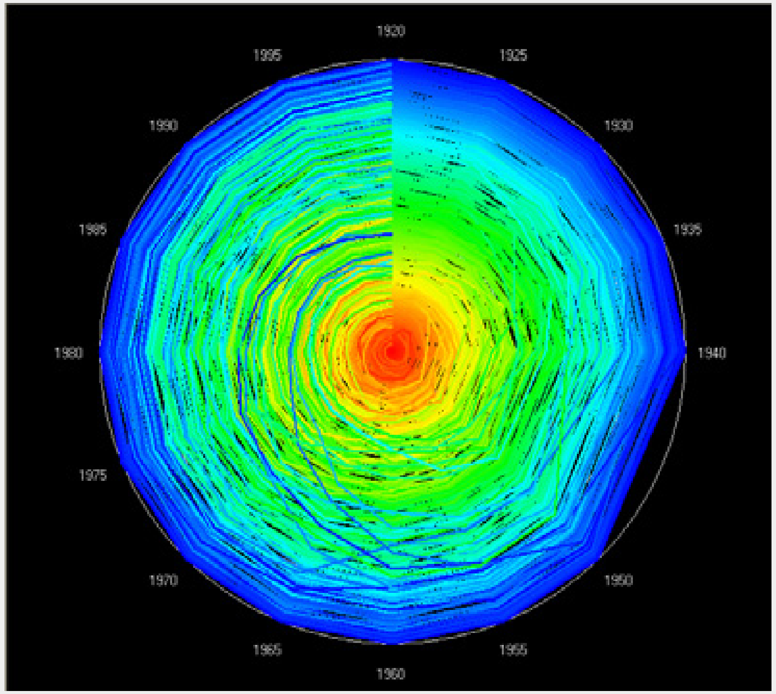
And we have these from 1920 to 2000 in five year periods

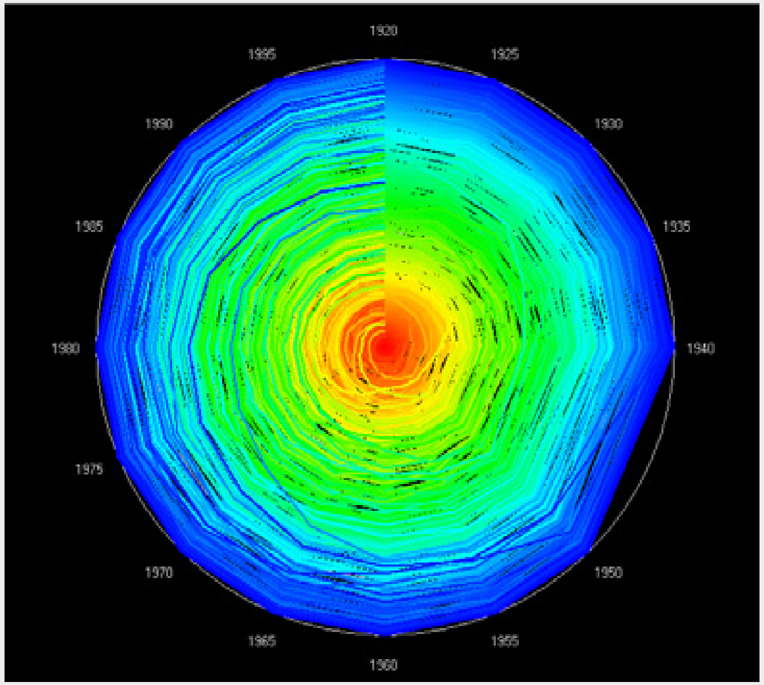
We will look first at the complete set of counts and then densities for 2137 and 269 and then look at Tokyo : first 2137 for counts and densities





then 269 for counts and densities

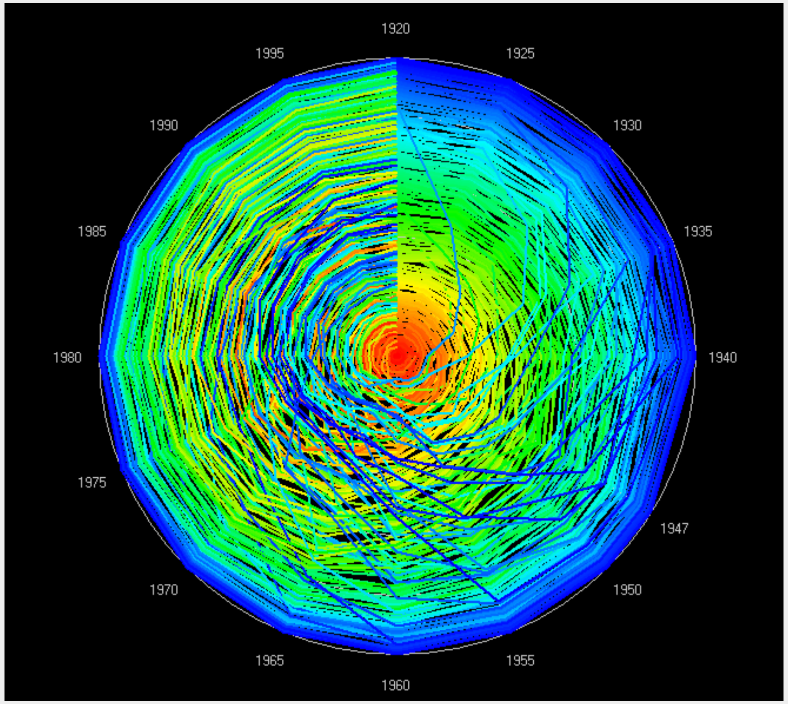


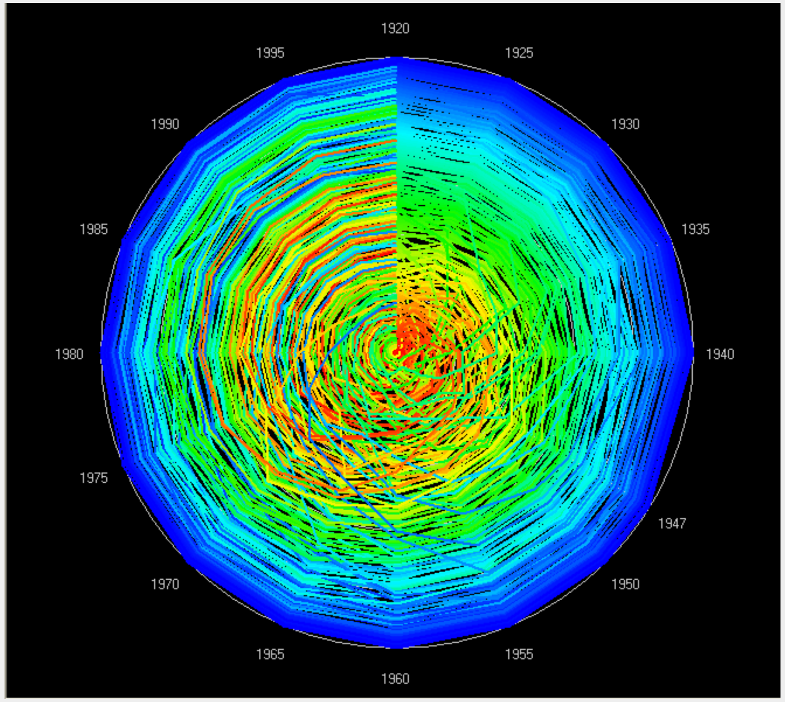


And let us look at the animation of the counts

RankClockJapaneseCities.exe
ucl

then Toyko, counts and densities,





Firm Sizes: From the Fortune 500

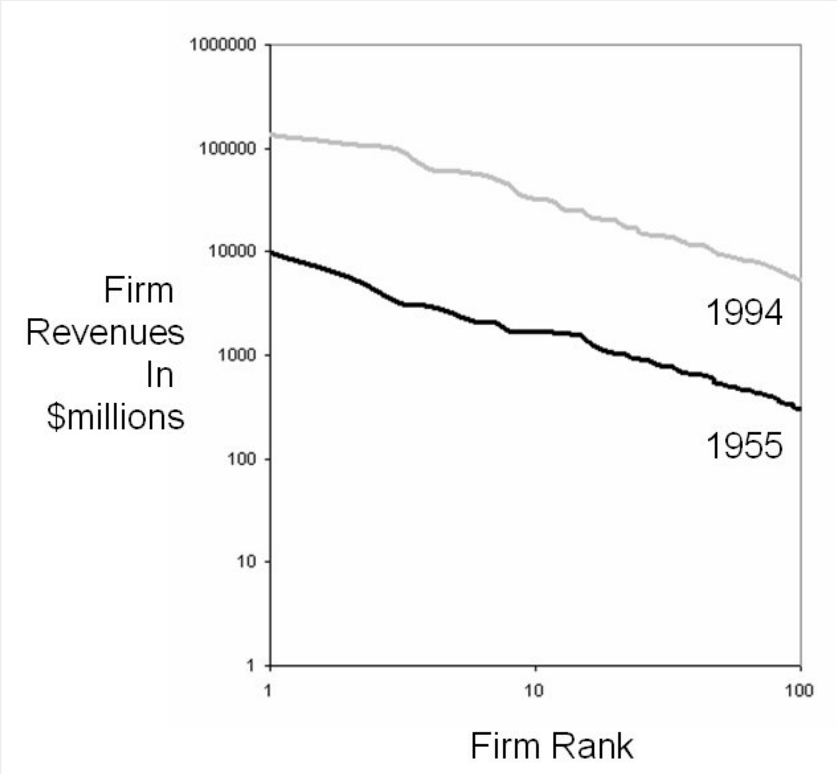
In fact we have taken the top 100 from 1955 to 1995 because the index was recalibrated in 1995

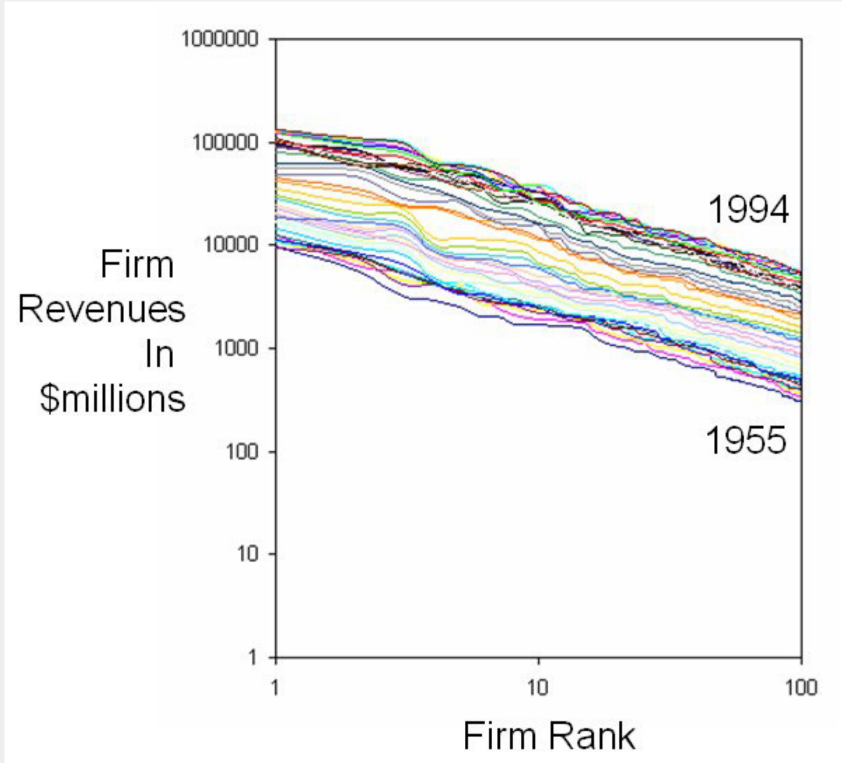
The data is available by revenue and by profit and we can thus compare these measures, i.e. their ratio

Essentially firm sizes follow power laws; but the degree of volatility is enormous – most firms in the top 100 in 1955 are now gone. Only 39 exist in 1995

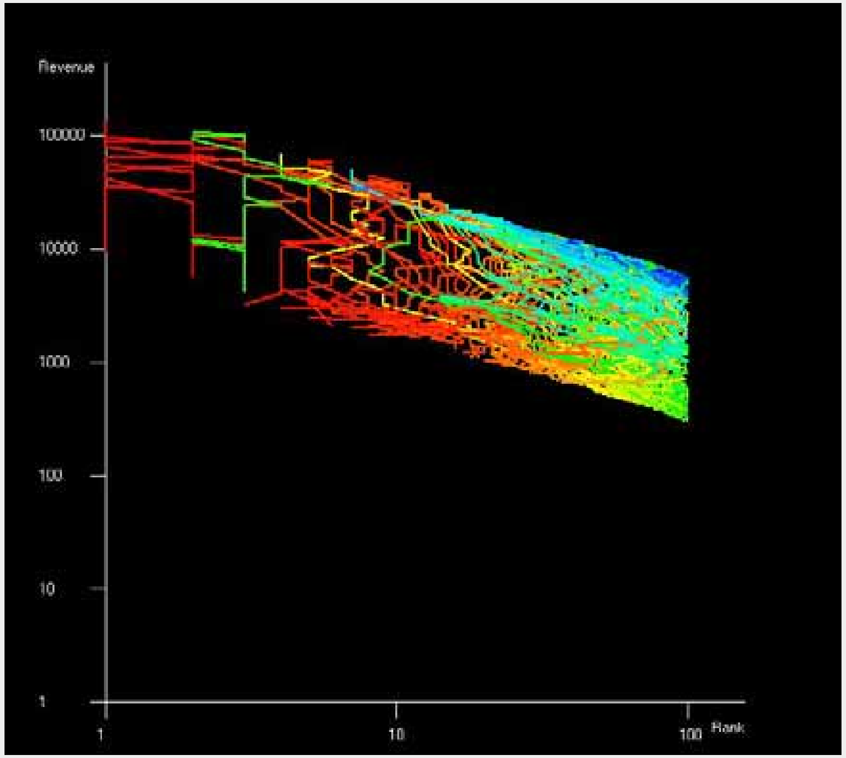
The picture is of a different growth dynamics – firms do grow and decline but they also merge and are acquired; they change their form in ways more complex, at least different, from cities buildings

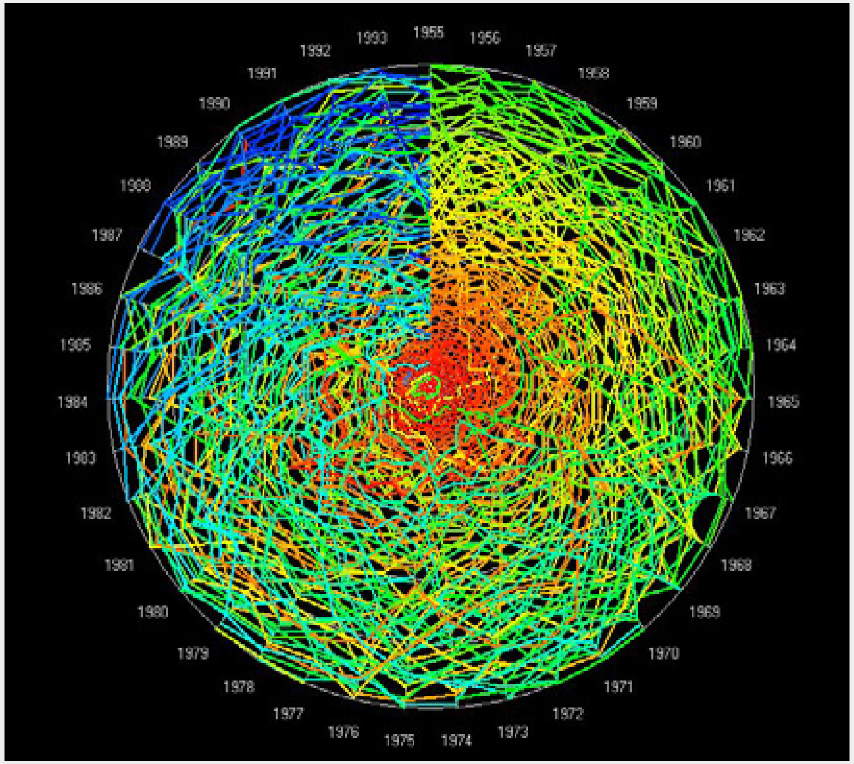
Rank-Size Relations



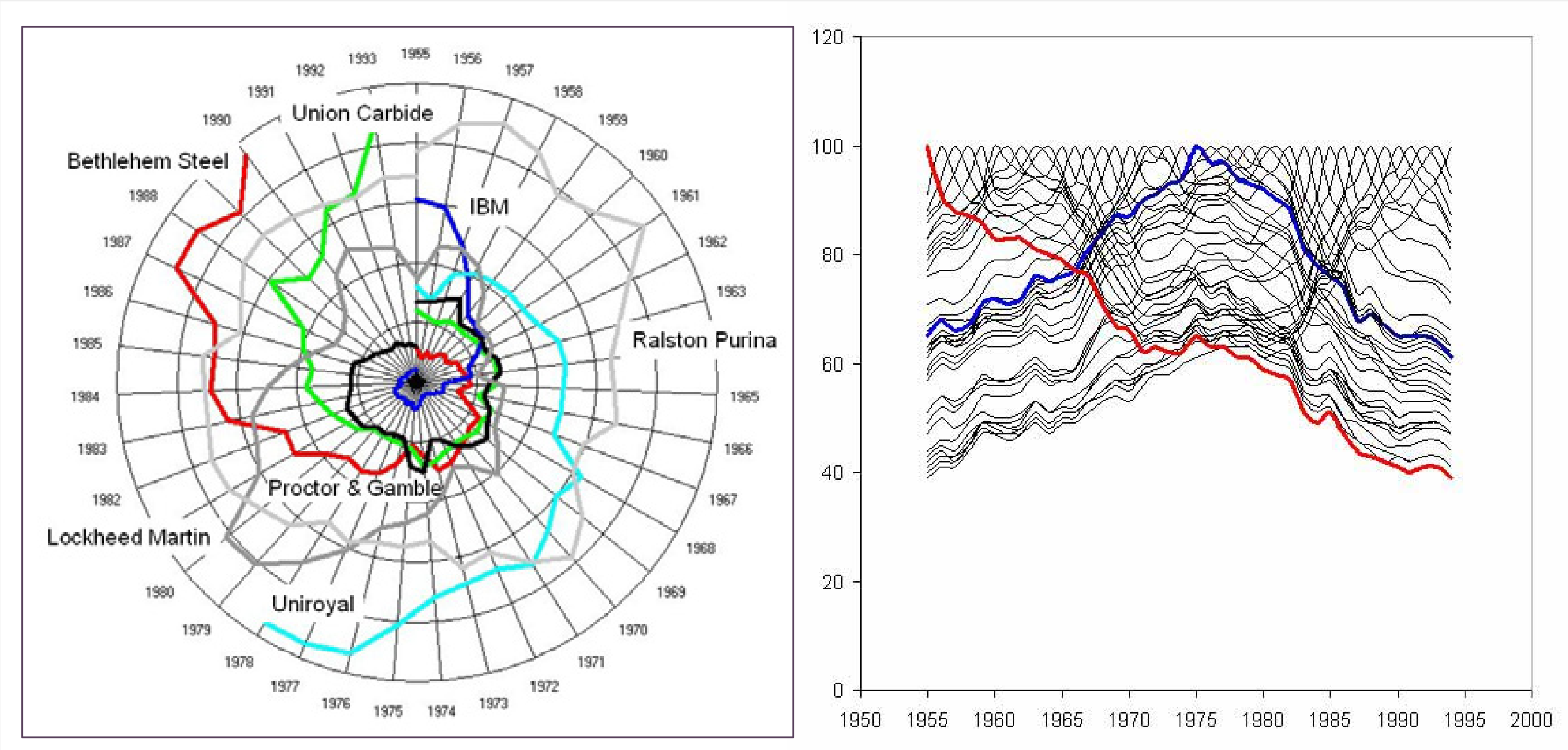


Rank Clocks and Rank-Size Space

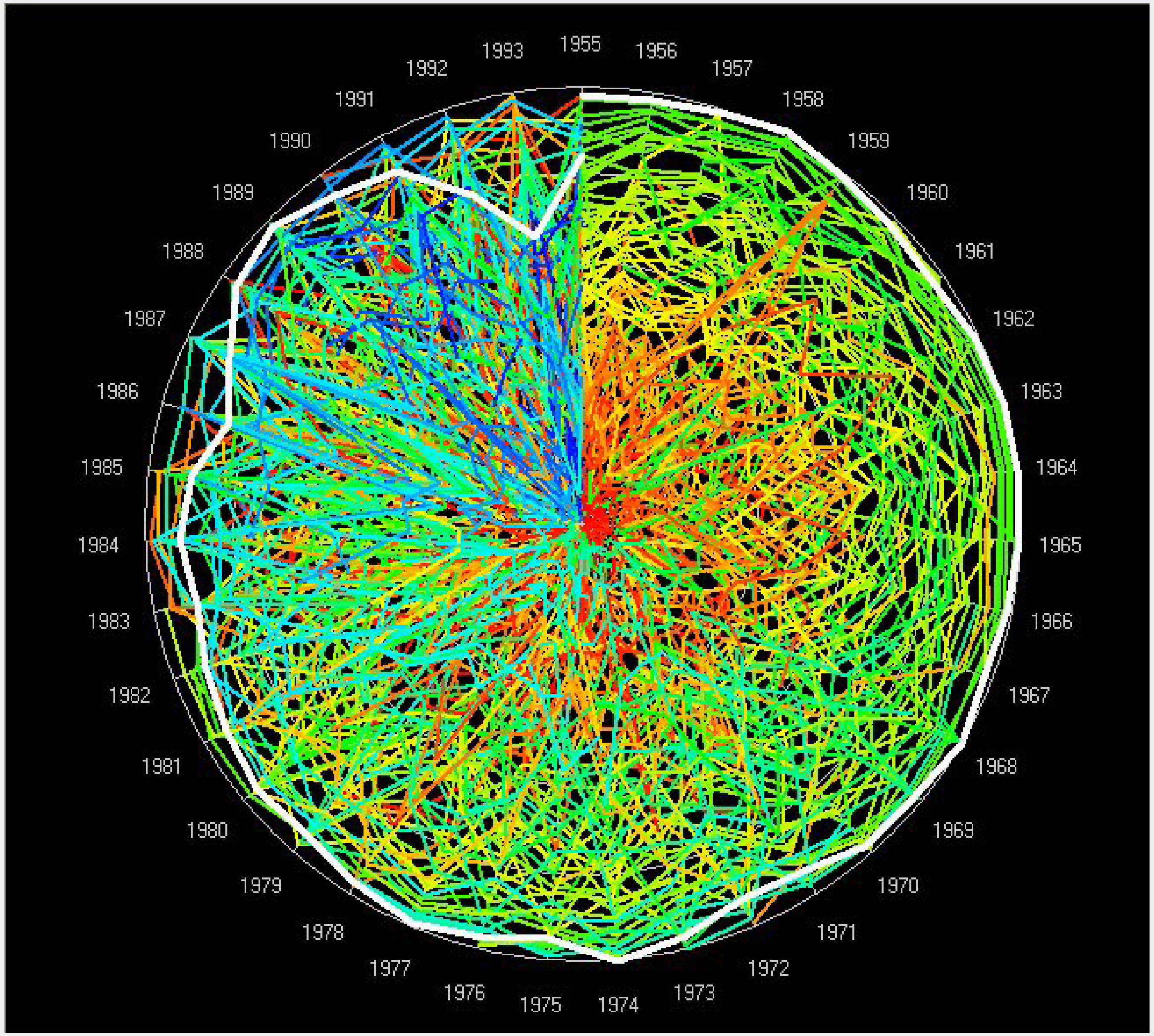




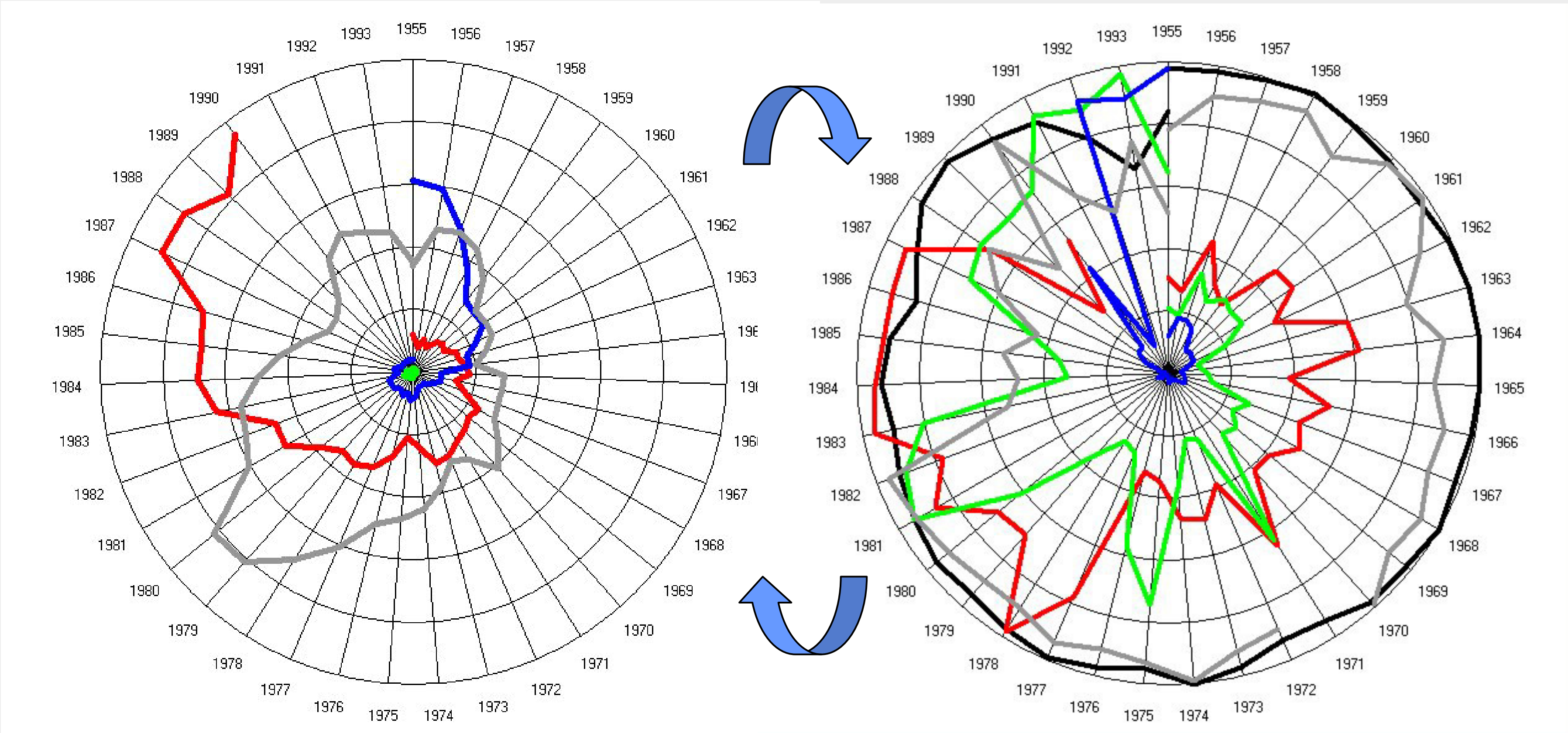
The Half Life: Firms: No of Firms in Top 100 Earnings/Revenues at Year t when all are in the Top 100 at Year τ



Rank-Size and Clock of Firm Profit Ratios



Earnings and Profit Ratios for Top Firms



Red – Bethlehem Steel: **Blue** – IBM: **Grey** – Lockheed Martin: **Green** – GM

Adding Place to Rank Clocks

Use OpenStreetMap as a base map

Use Google Earth browser plugin for 3D mapping

- Represent each point as an extruded pillar
- Create the pillar size and height based on the extent and average density of data

For simplicity, a uniform distribution of points across a square extent is assumed

Communicate with Google Earth by passing it KML

OpenLayers will readily convert any geometry to KML

Additional Options to Aid Visualisation

Inverting the rank clock

Limiting the size

Colour by:

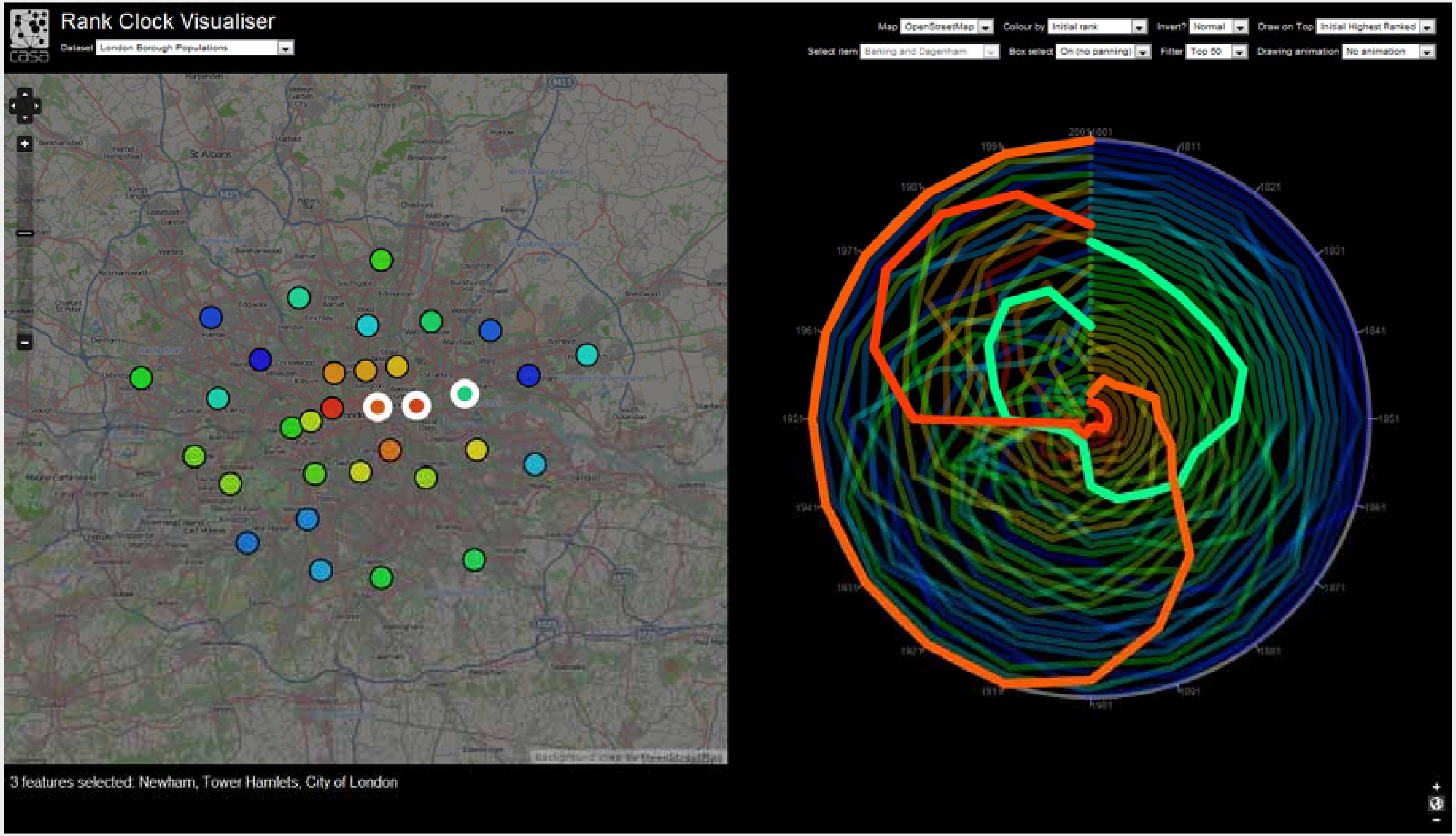
- Initial interval
- Initial rank
- Final rank

Layering the lines (painter's algorithm) by:

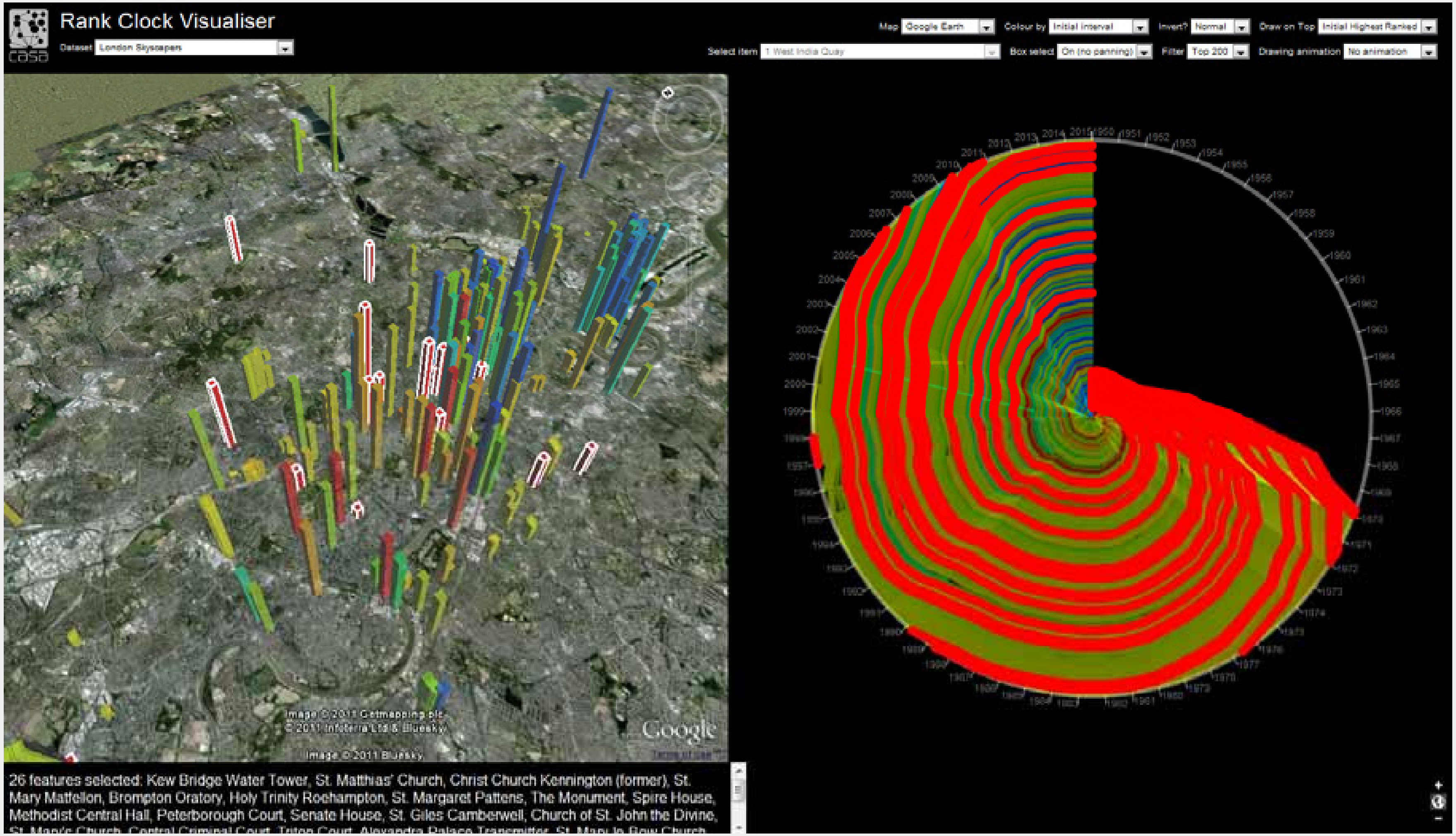
Initial or final highest or lowest ranked

The blog http://oobrien.com/2012/02/rank-clocks/ and the site http://casa.oobrien.com/rankclocks/

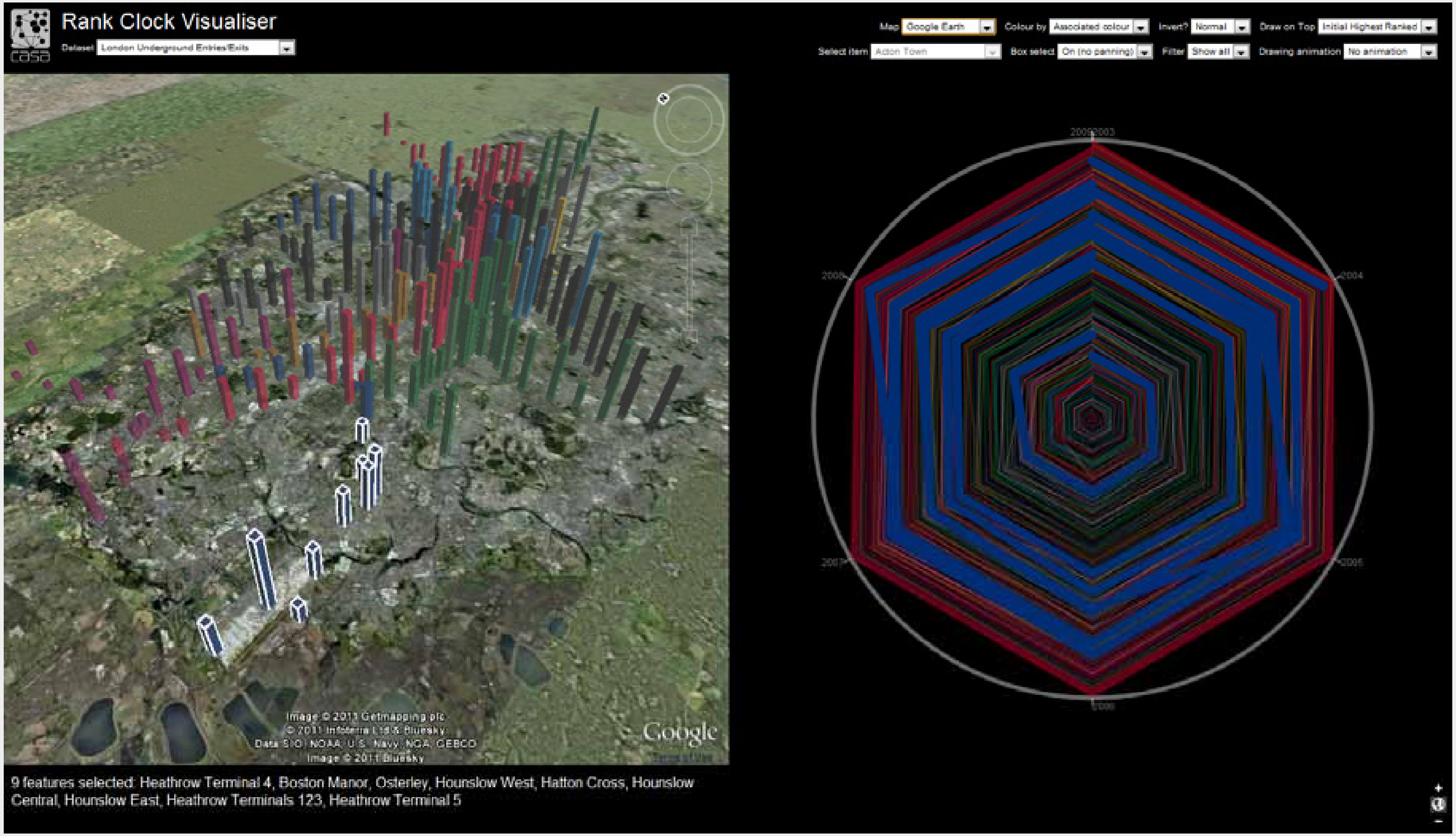
Demo – populations in 33 Greater London Boroughs from 1801



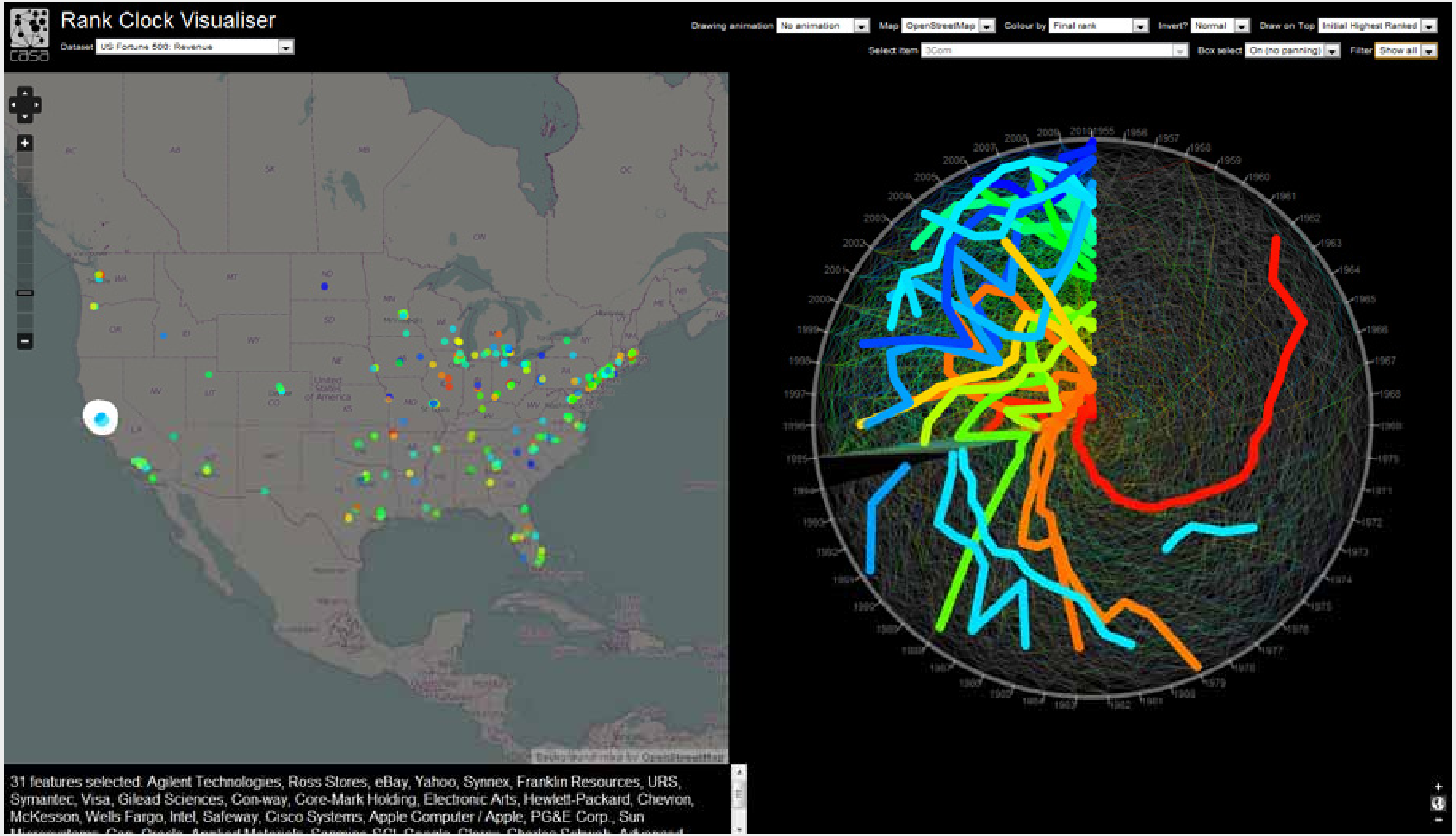
Demo – High buildings in London from 1950 to 2015



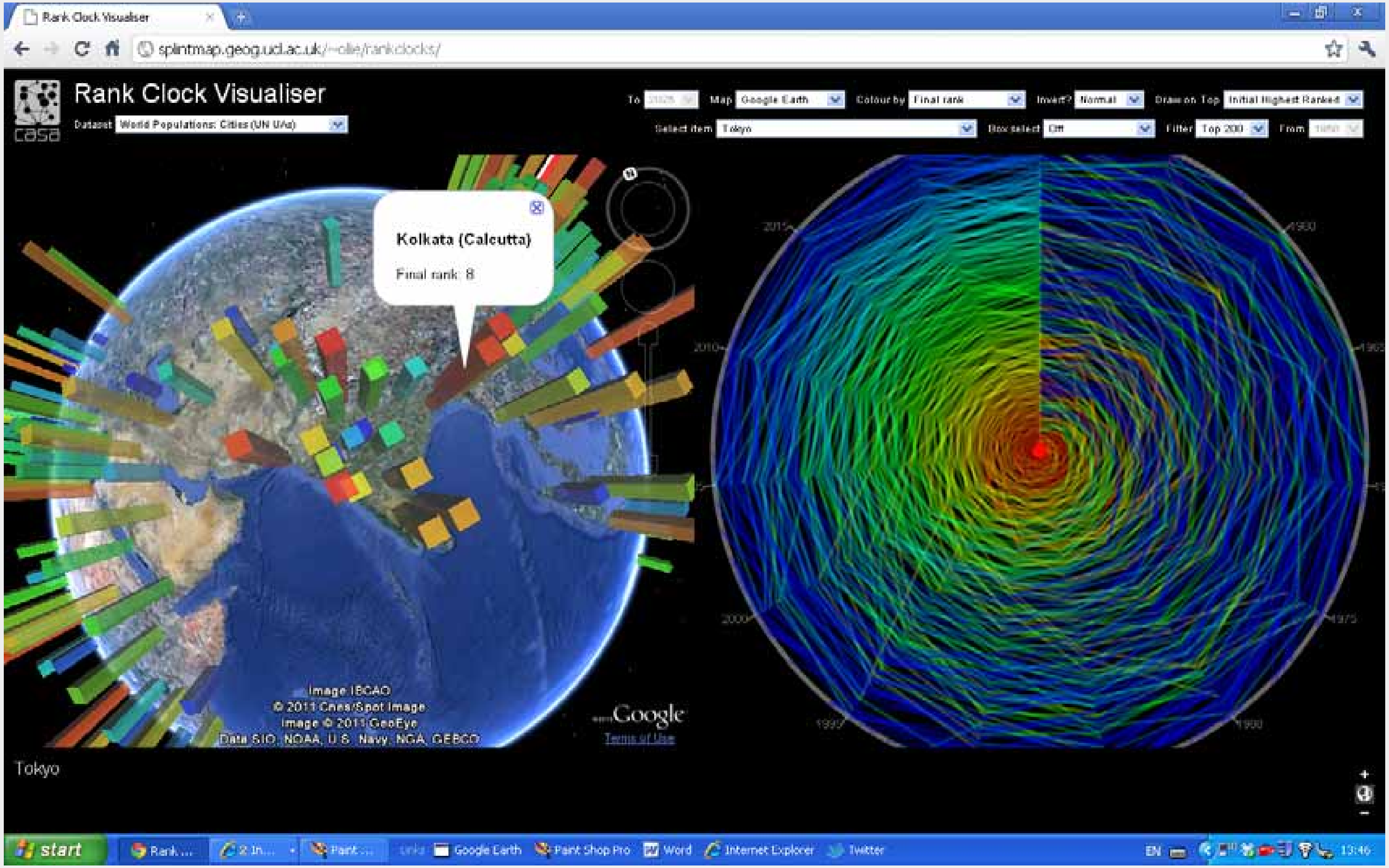
Demo – Tube Exit Volumes from 2003 to 2009

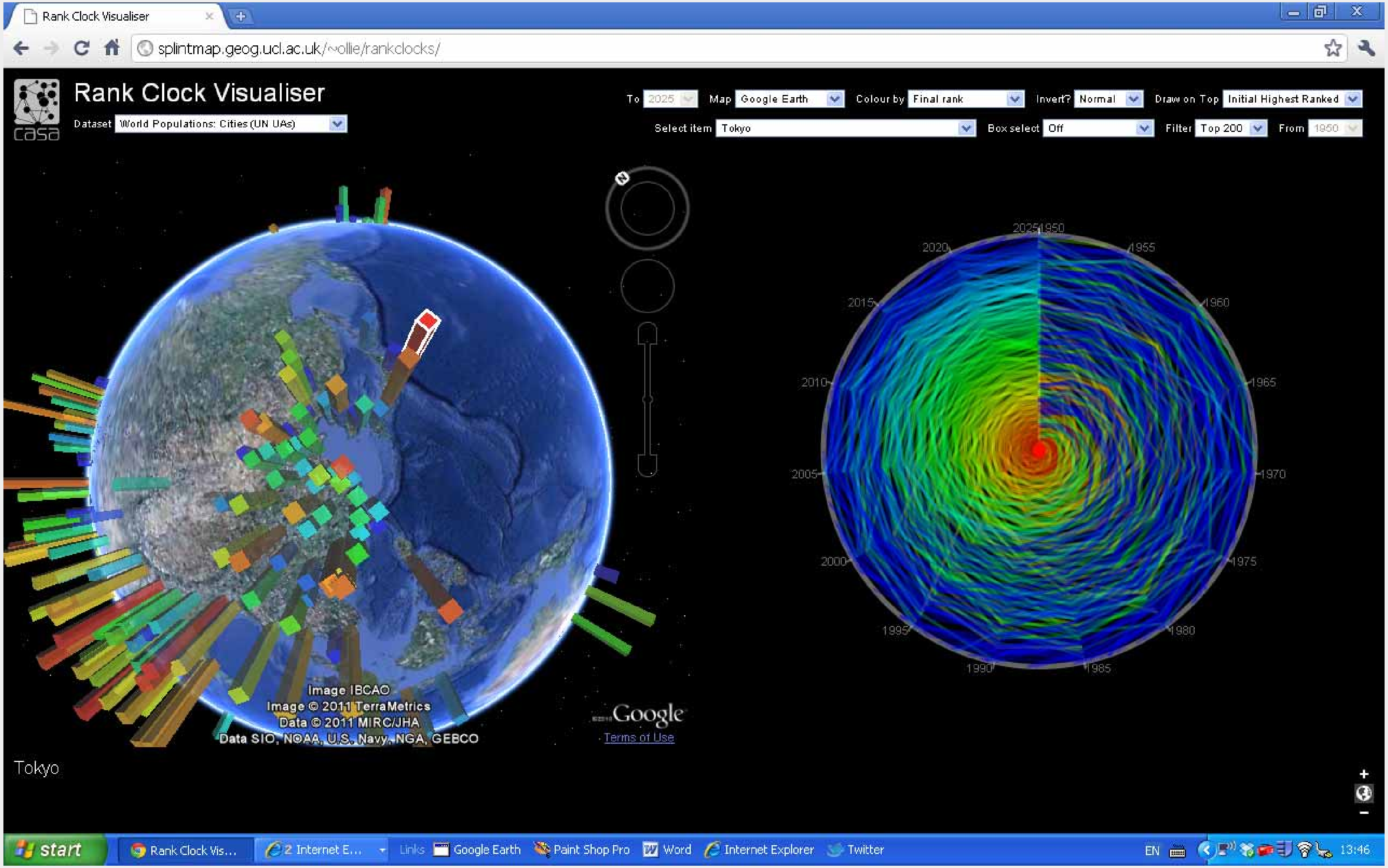


Demo – Fortune 500 from 1955 to 2010 for a sample of fast rising companies



For United Nations World Cities Population (595 cities) from 1950 to 2025

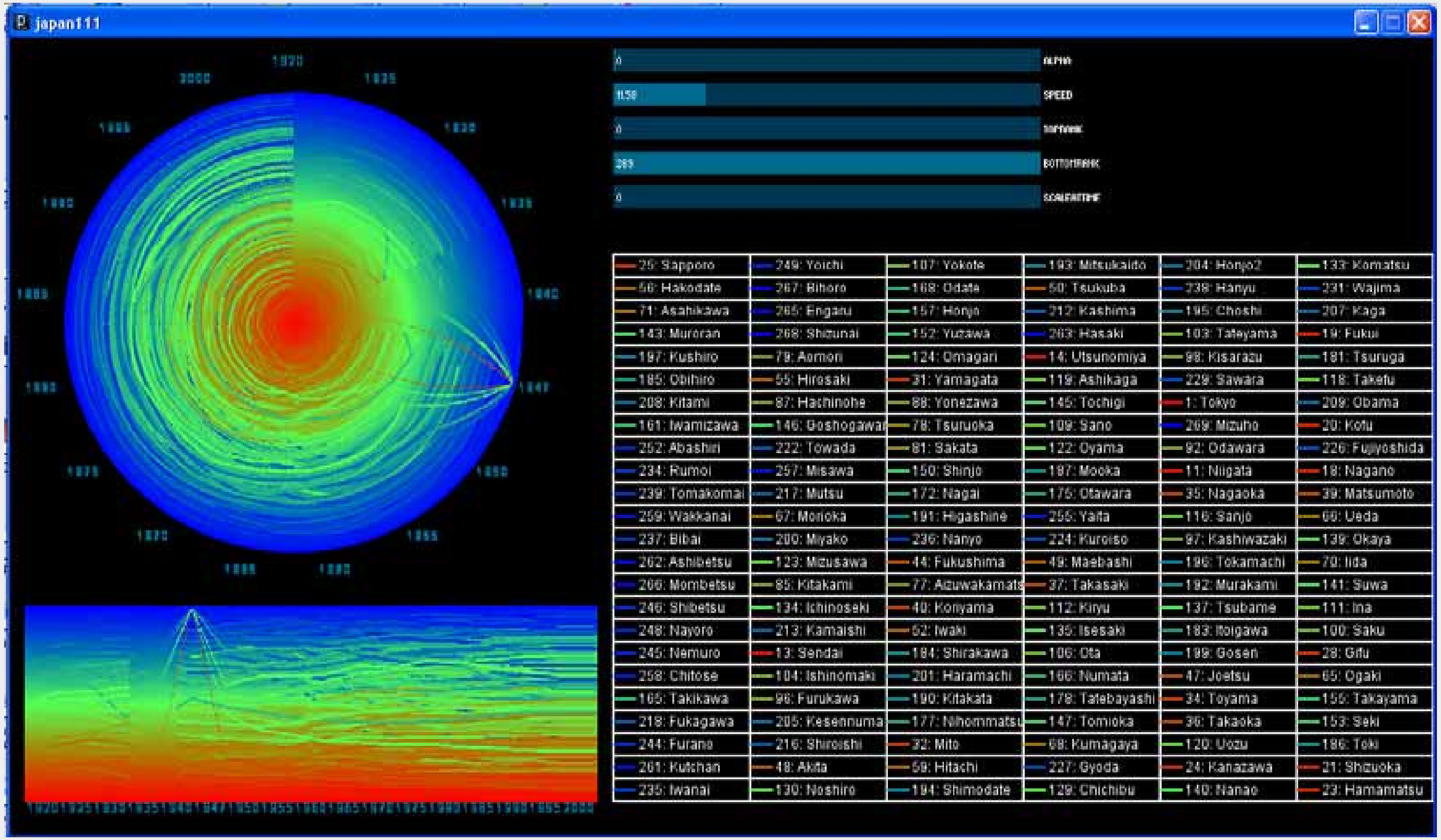



Rank Clock Visualiser
splintmap.geog.ucl.ac.uk/~ollie/rankclocks/
Rank Clock Visualiser
casa
Dataset World Populations: Cities (UN UAs)
To 2025 Map Google Earth Colour by Final rank Invert? Normal Draw on Top Initial Highest Ranked
Select item Tokyo Box select Off Filter Top 200 From 1950
Image IBCAO
Image © 2011 TerraMetrics
Data © 2011 MIRC/JHA
Data SIO, NOAA, U.S. Navy, NGA, GEBCO
Google
Terms of Use
Tokyo
2025 1950
1955
1960
1965
1970
1975
1980
1985
1990
1995
2000
2005
2010
2015
2020
start
Rank Clock Vis...
2 Internet E...
Links
Google Earth
Paint Shop Pro
Word
Internet Explorer
Twitter
EN
13:46

Animations: Rank Clocks and Rank Space

- Martin Austwick's has developed another set of programs which are superb at animation using *Processing*
- The essence of this is to continuously animate the clock and then we can see the deviations
- We can also plot individual trajectories and we can shorten the trajectories to show how each moves relative to one another
- We can do all of this also in rank space but I can't show you this

Here is the typical user interface. I can’t show it running as I don’t have the software here but you get the idea



Next Steps

- ***Good measures of the volatility***: some of these I have explored but as yet we haven't done anything comprehensive – such as distances measures on the clock – measures of spread such as entropy and so on
- ***Extensions to network systems*** – trade and migration and traffic flows and their changes over time – in terms of nodal volumes and flows on links
- ***Examining different definitions of cities*** – and related systems: cities as exhaustive partitions of space versus cities as nodes or points
- Some work on ***types of clock*** is being done

nature Vol 444|30 November 2006|doi:10.1038/nature05302

LETTERS

Rank clocks

3534 NOTES

Ecology, 89(12), 2008, pp. 3534–3541

RANK CLOCKS AND PLANT COMM

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Abstract. Summarizing complex temporal dynamics in
in a way that yields an intuitive picture of change. Rank cl
provide a graphical and analytical framework for displa
dynamics. We used rank clocks, in which the rank order ab

RESEARCH ARTICLE

Visualizing Space–Time Dynamics in Scaling Systems

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SCALING IN COMPLEX SYSTEMS

Objects or entities that define many complex systems often scale with respect to the frequency at which they occur in space and/or in time. Such scaling reveals an order in the system manifest in the fact that patterns recur over different scales, revealing what is called in fractal geometry, self-similarity. This is best visualized as some configuration of system entities that appear the same, at least statistically, from one scale to another, good exemplars being dendrites whose branches mirror the way rivers drain a landscape, crystals solidify, and liquids of different viscosity penetrate one another, all the way to how energy is delivered to the human body and how organizations arrange themselves in overlapping hierarchies [1].

Formally, the most general scaling, which captures the frequency $f(x)$ with which elements of different size x

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Questions?

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